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Sy'al N. Patel (19574234622) ECE

PM1(B) C. E

Dr. Chakrapani

Advanced Books Text Books

1 Samuel C. Lee Un Morris Mario.

@ Kohavi @ Tocci & Woolmer.

3 R.P. Juin

Digital Electronics

0 O (-) (<del>)</del> 0  $(\tilde{\phantom{a}})$ 

\* Basic Topics

- 1 Logic Jates
- @ Number System
- 3 Complementary Number depresentation and Binary Number.
  - @ Binung codes.
- 3 Booleum Algebra.
  - € K-maps.

A H B = A HB

All:

& Logic Crate:

-> AND, OR, NAND, NOR, EX-OR, EX-MOR getes.

-> NAND & MOR USE Universal gertes.

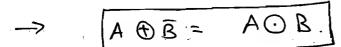
□ Equavalance | coincidence gete
 ⇒ Extor gete

| → A <u> </u> |            | Y-0<   |     |
|--------------|------------|--------|-----|
| (            | Y =        | A O B  |     |
|              | \ <u>.</u> | 7. R + | A.R |

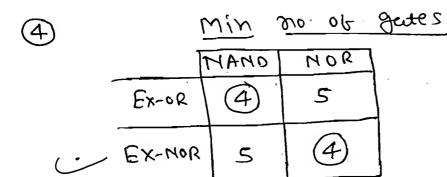
| A  | B   | 4   | - |
|----|-----|-----|---|
| 0  | 0   | 1   |   |
| 0  | 1   | 0   |   |
| ١  | 0   | 0   | じ |
| 1. | 1 1 | † , |   |

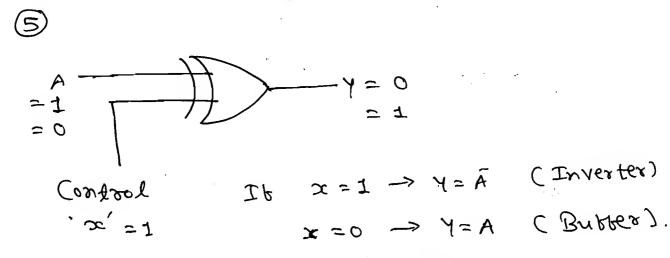
=> Ex-OR gente Logic

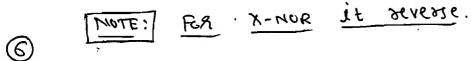
$$\begin{array}{c}
A & B & Y \\
\hline
A & B & Y \\
\hline
O & O & O \\
O & I & I \\
I & O & O \\
\hline
Y = A \oplus B \\
Y = \overline{A} \cdot B + \overline{B} \cdot \overline{A}
\end{array}$$

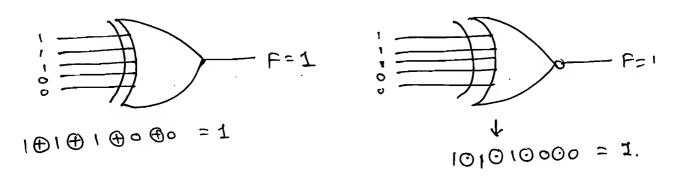


(\_)









NOTE: ]

NOTE: ]

Ex-OR output = 1 ib Input has odd nool is

E.g. = cABBOC = AOBOC.

Ex-NOR = EX-OR

it no. of Input Vanables

(I)

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are even.

E.g. = AOBOCOD = ABBOCOD

**3** 

Bubbled gestes (Negative gestes)

@ Bubbled OR gete = NAND gete

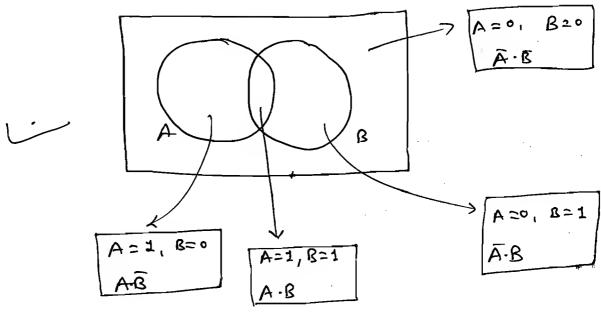
Bubbled AND gete = MOR gete

@ Bubbled Ex-OR = Ex-OR gerte

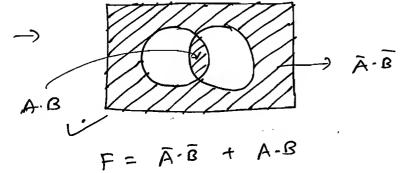
17

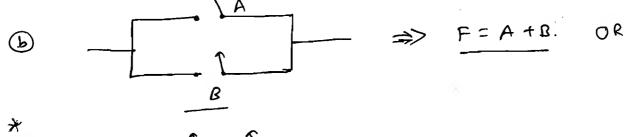
17

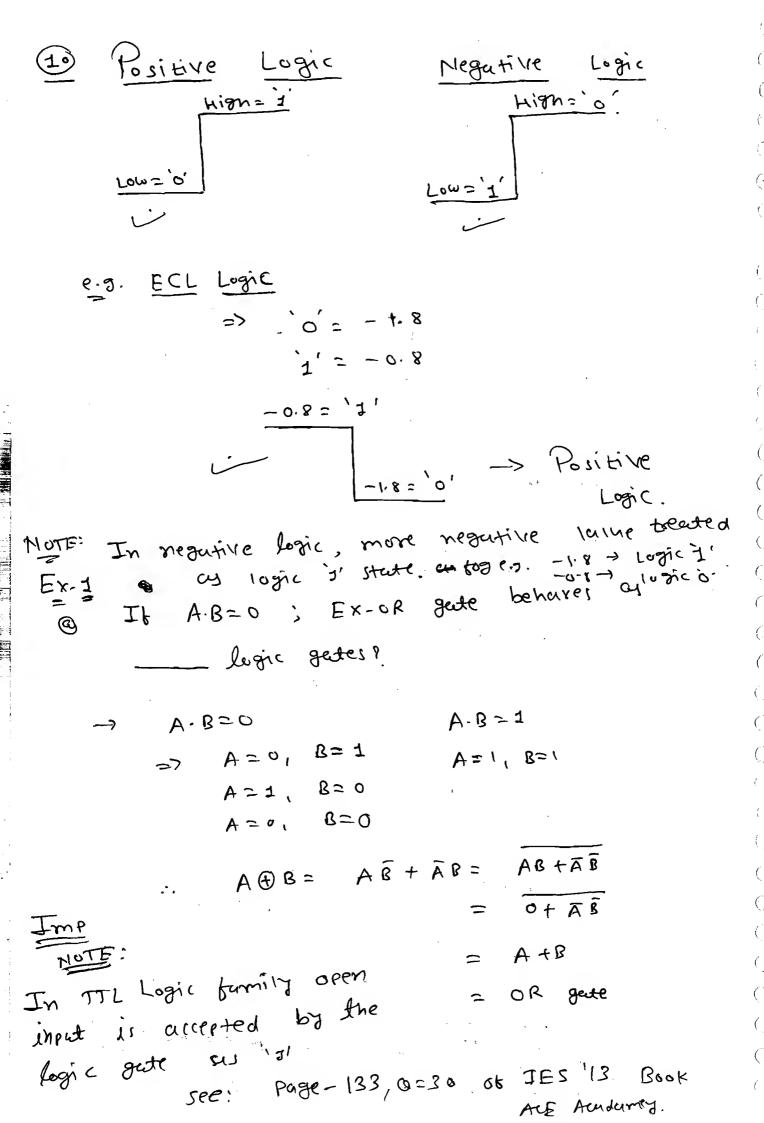
(C)

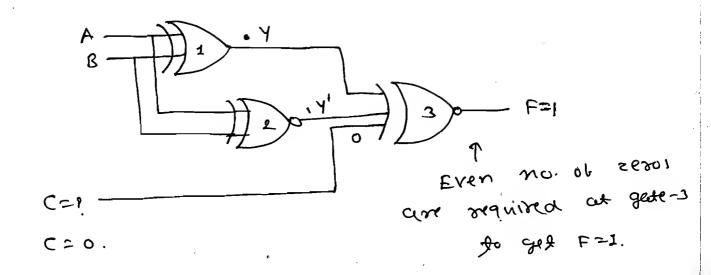


7

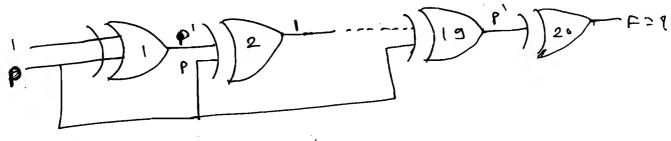








owent F= 8. © Fina



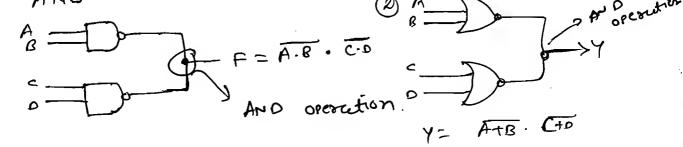
Page pol F = 1.

output at even gete is I and at oda gete is P'

After even no. gester -> or=>1) Alter 20 getes -> olp=1.

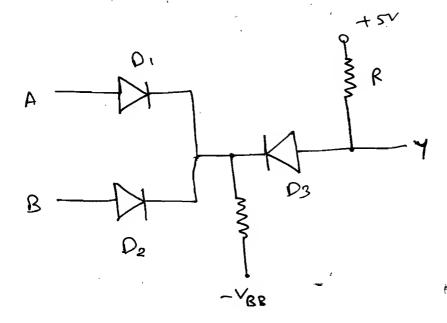
if initial condition is reverse Incor 1 become o fine it act as a butter.

NOTE: Open Collector TIL Will Provide wired. AND operation.



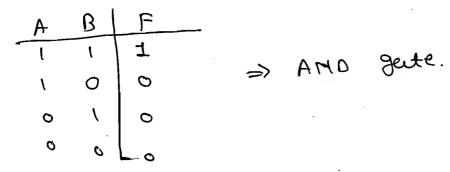
0

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 $\mathcal{F}_{\epsilon}$ 



MOTE: (i) tre logic or gete = -re logic AND gete

tre legic - re legic

AND OR

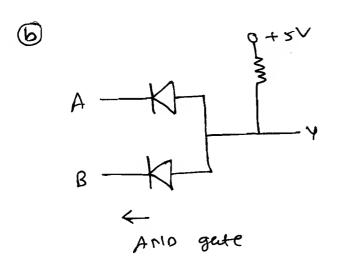
OR - AMO

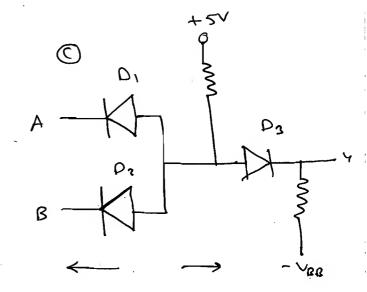
NANO --- NOR

MOR --- MAND

EX-OR == EX-PloR

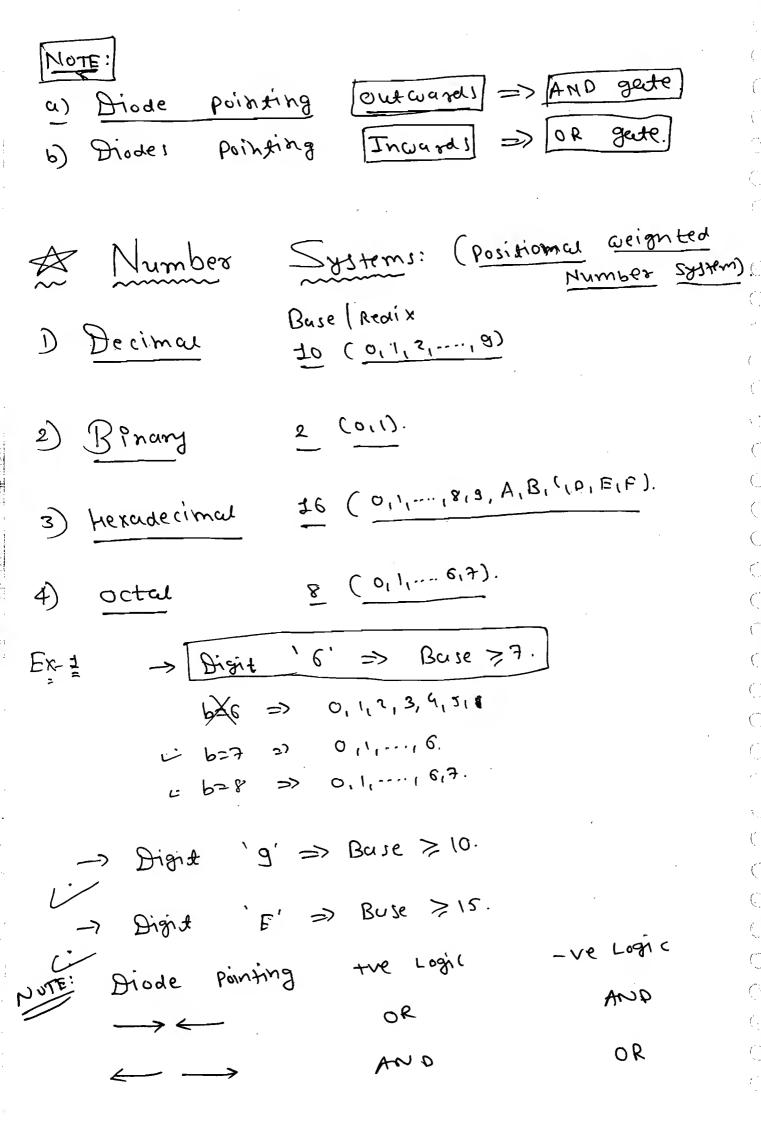
EX- MOR --- EX- OR.





I j

AND gate



Ams: (60. A8)16.

Ex ? How many bits are required to sepresent 6728,0 in binary.

Ans:  $2^{n} > 6728_{0}$  n = 13 bits.  $2^{12} = 4096$ 

213 = 8192

$$Ex-\frac{3}{2} \quad 6728_{10} \longrightarrow x_2 =$$

$$\frac{16 |6728}{16 |420|} = (6728)_{16} = (6728)_{10}$$

$$\frac{16 |420|}{16 |26|} = (6728)_{10}$$

NOW, 1 A 4 8

(8578) = (0001101001000) E

How many bits are required to depresent Ex- 3 a 32 digit decimal no. ?

Ans:

$$2^{\gamma} > 10^{32}$$

ninz > 32 luio n > 32 ( In10 ).

w > 106.30 => [w=10]

Ex-4 Determine the buse of the bollowing sercions.

@ 24+17 = 40 => max digit =7 Hence buse>8. Let, base = ba

(2b'+4b')+(1b'+7b')=(4b'+0).26+4 + 6+7 = 4b.

Mote:

$$AF_{16} = \frac{3x_{81}}{10x_{16}^{1} + 15x_{16}^{0}} \times \frac{10x_{16}^{1} + 15x_{16}^{0}}{10x_{16}^{1} + 15x_{16}^{0}} \times \frac{10x_{16}^{1} + 15x_{16}^{0}}{10x_{16}^{0} + 15x_{16}^{0}} \times \frac{10x_{16}^{1} + 15x_{16}^{0}}{10x_{16}^{0} + 15x_{16}^{0}} \times \frac{10x_{16}^{0} + 15x_{16}^{0}}{10x_{16}^{0}} \times \frac{10x_{16}^{0} + 15x_{1$$

```
    √ 41 = 5.
```

-> Let, Base= b.

14xb + 1xb = 5xb

: 46+12 25

46- 24

-- H=19, b=6

Roots of x2-11x+22=0 are 3 and 6

b= ?. Max digit = 6, Baje >,7.

Fus:

×(x-3) (x-6) = 6

81+ xe-2x xis

lex, souts are x=3, x=6.

x1+x2 = - 6/a.

3 part 6 par - (-11) = 11 pure

: (3 x base)+ (6 x base) = (base + 1)

3+6= buse+1

buse= 8

(Or)

x, x22 (a.

: 36,x 66= 22 = 226,

 $3 \times 6 = 2b, +2.$ 

: 18 = 26,72

26,216

(b1=8)

Ex 5 What is the min decimal value of 11cx = ?

max digit (, so buse > 13.

Ams: 
$$(x^2 + x + 12x^6)_{10}$$
 Base >, 13.

min decimal occupes when base is minimum i.e. b=13.

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(3)

(i)

$$= 13^{2} + 13 + 12$$

$$= 19 + 10$$

$$\frac{1.24}{2.34} = \frac{1.2}{(10.1)_4}$$

$$\frac{1.(2x.4^{-1})}{2.34} = \frac{(2.75)_{10}}{4.25}$$

$$\frac{2.34}{(10.1)_4}$$

$$0.25 \times 4 = 1.0 10.(27 + 1.0)$$

$$=1 10.1.$$

$$\frac{5(x_1)^{\frac{3}{2}}}{4300} = \frac{300}{24} = \frac{8124}{13} = \frac{8124}{16} = \frac$$

Ex-8 A

$$B = 11$$

$$0 = \frac{(3)}{(24)} = \frac{16|24}{1} = 8$$

$$(18) = 6$$

$$D = 13$$

$$E = 14.$$

$$11_{11} \Rightarrow 17_{10}$$

$$10 = 3$$

$$10 = 29_{10}$$

$$-E_{11} = -19_{10}$$

$$F_{11} = 17_{10}$$

Domplemetary Number Representation:

A - B = A + (-B)

A-B = A + ( comprement of +B).

Base = 92' system

-> (9-1)'s Complement => 9n-9-N

→ R'S Complement =) 2<sup>n</sup>-N.

N= criver Number.

n= no. of digitis in Integer part of N. €

m= no-06 divitis in Fractional part of N.

E.g.: Find 9's Complement of 835.271, 29

&= 10, N= 835.27, method-1

: n= 3, m= 2.

103 - 102 - 835-27

= 1000 -0-01 - 832.53

= 164.7210

Ex- & 70,2 Combiement (325)11 = 6

19

(35 2)11.

&=11.

we have to find

(2-1) 1 Comp.

$$\frac{2}{5}$$
 Gmplement  $\frac{2}{5}$  Comp. of  $x = 101101000$ 

Apri:  $\frac{2}{5}$  Com: 010011000

$$Ex-4$$
 01102 - 00012  
 $610-110$   
Ans: 01102 + (complement of 0001).

$$\frac{By}{O|_{1}O_{2}} = 6|_{0}$$

EAC 1110 = 113 Complement of 00012

EAC + 1111 = 215 Comp. 06 00012 EAC = 510

EAC = En

EAC = End Around cary.

0

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MOTE:

FAC doesn't occur when the result is

-ve. i.e. Large value is subtracted from

a Small raime.

A Binary Numbers:

> 1) Unsigned numbers. > [n bits]

2) Signed numbers. > [magnitude]

magnit

(n-1) bits

MSB

Sign bit

0 -> +ve

1 -> -ve

=> @ signed magnitude form.

1 6 1's Complement form.

2 0 21s Complement form.

C 2's Complement born. + 510 = 01011 - 510 = 2's Comp. of + 5. - 540 = 1011.

Ex-1 Represent the tolowing no. in 215 complement to91m:

a) -1710 b) -83.37510.

Ans: a) +17,0 = \$\$\$010001

-1710= 2's comp. of +17.

= 101111 -- 128 64 32 16 8 4 2 1.

b) - 83.37510

→ 83.332 = <del>0110001</del> 01010001.011

$$\Rightarrow -83.3750 = 215 Camp. 06 + 83.3750$$

$$= 211 Camp. 06 + 83.3750$$

Determine the decimal values represented by the following signed no.s.

- BYXXX VS SYST
  - 1) sign maj. no. 1101 is -510

2) (a) 2's comp 01110 is +14

6) 1'1 comp 200 01110 is +14

3) 2's comp no, 11001'=> --- 9.

5) 1's comp. no 10010 is - ?

GATE

(1) What is the eanuvalent 215 camp. represententation Ot a 2's comp. no. 1101 is - ?

215 camp. no. -> orack! (101. =) -3 c+3.

(A) 101101 -1910

\*(B) 001101 → +U1.

111101 215

~ (c) 111101 → - 310

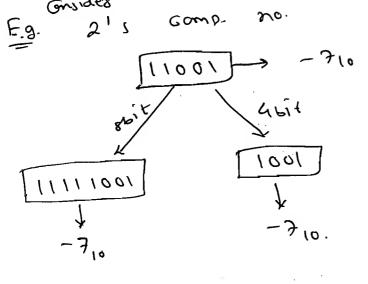
= 0000 pl - -3.

x (D) O11101 -> +2910

\* Sign bit Extension:

-> In i's 82's complement tom the Sign bit can be extended towards lett any no ob limes without changing its

Value.



Exi A 2's Comp. 200. "X4 X3 X2X1" Is

Exi A 2's Comp. 200. "X4 X3 X2X1" Is

Copied into 6-bit register which of

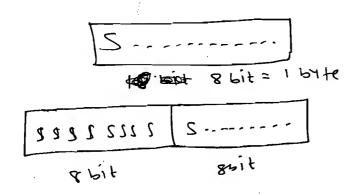
the following indicate the value of the

register.

()

- @ 11 x4 x3 x2 x1.
- B X4 X4 X4 X3 X2 X1.
  - ( 00 x4 x3 x2 x1.
  - @ Mone.

\* Converse Brite to word ( CBW).



2) Contere Word to somble word. => (CWO).

16 bit 32 bit

Ane vaine of the seg.

Ans 1

10100

= -16+4= -(2.

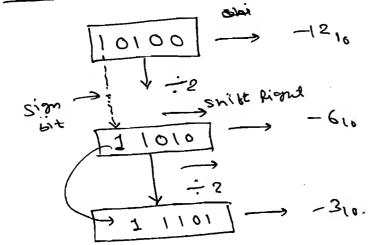
 $\frac{-12}{2} = -6$ .

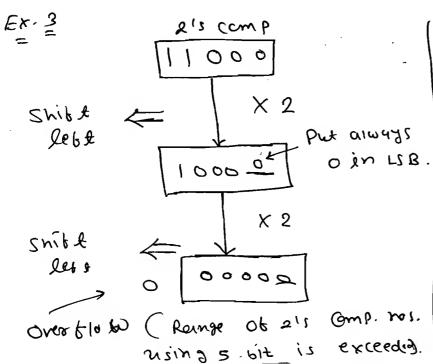
 $\frac{2!}{-6} = \frac{2!}{5} \quad \text{Comp.} + 6$ 

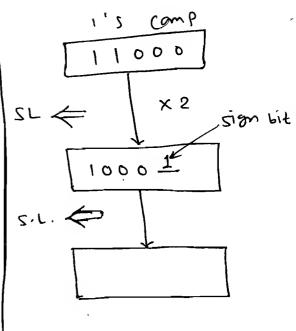
= 215 Comp. 00110

= 11010

-> method- 2:









Range of onmber represents using n' bits.

J's Comp. form , sign mag. tom  $+(2^{n-1})$  to  $-(2^{n-1})$ .  $+(2^{n-1})$  to  $-(2^{n-1})$ .

215 Comp 6092m

 $+(2^{n-1})$  to  $-2^{n-1}$ e.g.  $n=5 \Rightarrow +15_{10}$  to  $-16_{10}$ 

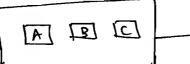
Reinge of sign mag. form.

= Reinge ob 1's Comp. form.

A Binary Codes:

7 bit ASCII code in sevice tashion.

(·;



2000 -> 30H = X 01100002

A => 41H = \$ [10000012

'a' => 61h = \$\\[ \begin{picture}(110 0.001\_2) \\ \ext{110 0.001\_2} \\ \

27 (1) Alphanumberic Codes. Numeric Codes. (2) -> ASCII Gde (7 bits; 27=128 Alphymumenal Alphanumenc codes (od e \*EB(OIC C & bit = 28 = 25 & Alphanumerical) IBM Computers. -> used In 2) Numeric Codes: -> BCO (Binary Coded Decimais) Codes. Non-weighted codes weighted Crouy code (Unit distance code) negativery Positively → 8 4 -2 -1 (ode. 8421 (ade Code. → 63 l -1 -> 5421 ->33 2 4 21

Selb Complementy Godes

sum of weights = 9

| Decimal<br>Digit | 84 2 1 | Excess - 3 |
|------------------|--------|------------|
| 0                | 0000   | 0.011      |
| 1                | 0001   | 0100       |
| 2                | 0010   | 0101       |
| 3                | 0011   | 0110       |
| 4                | 0100   |            |
| 5                | 0101   | 1,000      |
| 6                | 0110   | 1,00       |
| 7                | 0111   |            |
| 8                | 1000   |            |
| 9.               | 1 001  | 11100      |
| myand 10         | 1010   |            |

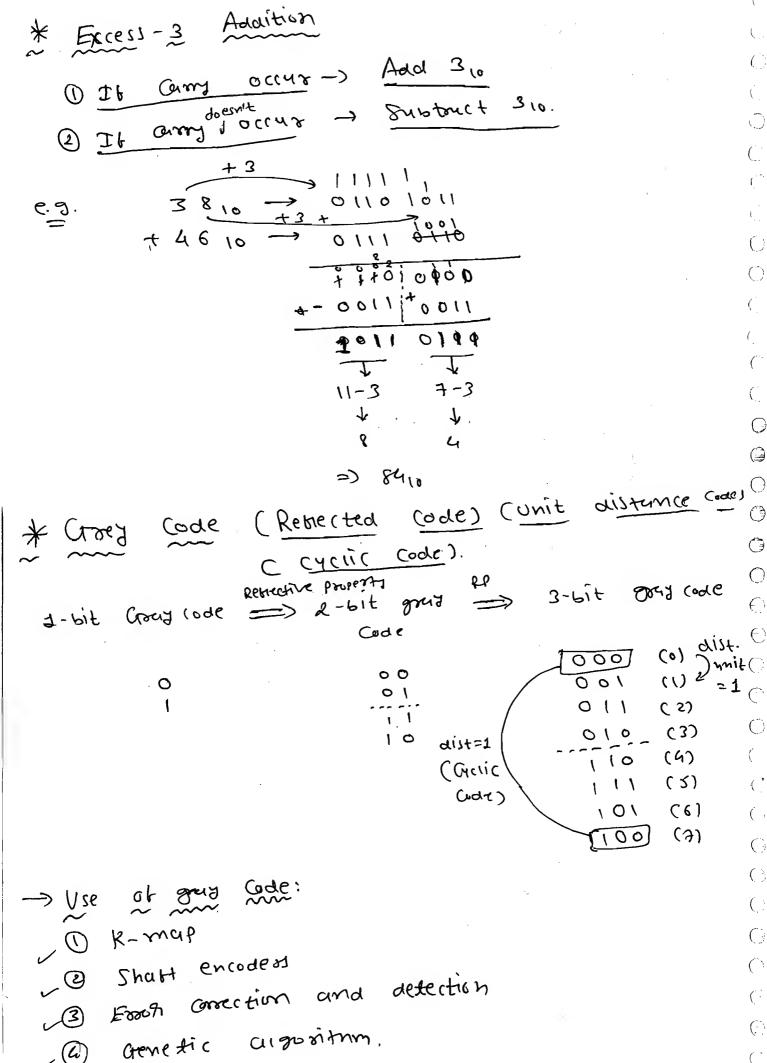
$$\frac{310}{310} = \frac{8421}{310} = \frac{110}{310}$$

$$\frac{310}{310} = \frac{310}{310}$$

29 -> The advantage of Ex-3 (ode is It is both segmential and selb complementing. -> During BCD addition output is invarid (1) It the result is greater than 9 (2) It Grong occurs during BCO addition 1110 carry =1 -> Invalid -> 0110 1000 E.g. 6810 + 0101 1000 +5810 11000000 + 0110 0110 Ans -) 1 26,0 (2) Find the no. of BCD Greetion = 8. + 1000 00100110 10011001 >9 × T. J. 10100000 So, 3 correction 0110 0000 101000000000 0110 0000 0000 0000 0000 0000

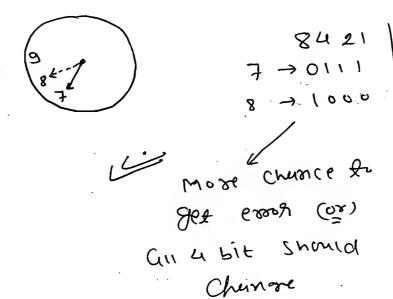
= 10000

0 0 0



-> Shutt encodess

1



Less Chance to
get coors cor
it is Unit distance
code.

asna code

010011

1100

by 🎉

& Code Conversion

1 Binary to Cour.

By By By By B,

Binary: 1 0 1

Crowy: 1 0 Cz Cr,

 $C_{1} = B_{1}$   $C_{2} = B_{1} \oplus B_{3}$   $C_{2} = B_{3} \oplus B_{2}$   $C_{1} = B_{2} \oplus B_{3}$ 

& Binany. (2) (roay cre Crz Crz Bu= Cra Gray: B3 = B4 @ C5 Binan: B2= B3 @ Ui  $B_3$ BI BZ B1 = B2 @ U1 B4

0

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Represent (743)8 in cony code.

(743)8 (111 100 011)2

NOW 8: 111100011

Cr: (100010010)

: (743) 8 = 100010010 + asal code.

Converter. Ode Briwonog Identity x4 the Ex-3 K3 74 = X4 43= xr ⊕ x3 Y2= x4 @ x3 @ x4 () Y3 = xn (1) \*3(1) ×2 € ×1. & G -> B

Ex-3 by b3 b2 b1 is a 4-Bit binary no. 33 What is the for of the following ents. b, bz b3 b4 (1)  $b_{ii} = b_{i}$ . 1 b22 = b1 ( b2. b33 = (b1+b2) ⊕ b3. 0100 b4 = (b(+b2 + b3) + b4. 1010 So, Ans is 215 comprement. (bitbeth) (by bzz b11 bun b33 \* Hamming Code Csingle Erroge Conrecting  $\Rightarrow 2^k \geq m + k + 1$ m=200.06 message bits. K= no- of parity bits. F.g. M=4 No. ob Parity bits [k=3] Let, Pi, Pz, P3. let, m,, m, m, m, m, 00,1-010 011/100 101. 110 111 2°= 1 21=2 3 23=4 5 P. Pz m, P3 m2 m3 m4 Choose Pi such that 1,3,517= Pi, mi, me, mi has oad i Choose 'Pe' such fact 2,3,6,7= P2, m1, m3, m, "", 10 Chouse 'Pa' such that 4,516,7= P3, m2, m3, m4 hus oad

```
Ex-1 (7,4) hamming Gale with odd parity
   for the message 1001.
      7 = total no ob bits.
    4 = no. or message bits.
                  3 4 5
                              6 7
              2
                      P3 0
                               0 1
                  1
             PZ
         ρ,
 Choose P, = P, , 1, 0,1 Should have parity => Cho
                          =) Choose [p=1]
      1,3,513
Choose P2 2,3,67 = P2 101
                                                  ()
                                  P2=1)
                                                  ()
Choose Pg 4, 516, 7 = P3 001
                                                  0
                                P3=0)
                                                  ٠
                                                  0
                                                  0
  Corrected code: 1110001
                                                  0
 (7,4) code humming ode is received as
                                                  \bigcirc
     1110101
        4,5,6,3 => 0101 => even panty => c3=1
                         > oda panty => (2=0
        2,3,6,7 => 1,1,01
                          a even punits =1 Car-1.
        1,3,517 = 1,1,1,1)
                             (in erroge)
                                                  ()
    1.e. essen occurred at (3 GG = 101 = 5th polition.
      Received Code = 1110101
                               tounsmitted (ode
                                                  (
      Corrected code= 1110001
                                 = 1001.
```

| => For Hamming Distance   |      |
|---|------|
| a) For Correcting   |      |
| l'errors: Hamming distance > 2  | t+1. |
|   |      |
| b) For detecting  | ++1  |
| 't' errors: Hamming distance >  |      |
| A   |      |
| Boolean Algebou:  |      |
|   |      |
| 14NO 100  |      |
| Identity 1' element =)  | ,    |
| A.0=0 A+0=A   | /    |
| A-11=A A+1=1.   |      |
|   |      |
| © Commtative Lew:   |      |
| Due A+B = B+A.  A-B = B.A.  |      |
|   |      |
| NAND:   |      |
| ATB = BTA   |      |
| $\therefore  \overrightarrow{A \cdot B} = \overrightarrow{B \cdot A}$ |      |
| A JB = B + A  |      |

$$\widehat{A} \cdot \underbrace{B}_{\underline{\beta}} + \widehat{A} \cdot \underline{C} + \underbrace{B \cdot C}_{\underline{\beta}} = A \cdot \underline{B} + \widehat{A} \cdot \underline{C}.$$

- ABCI+C) + ÂCCI+C).

= ABTAC

0

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```
[x.A + A.5] = 2xA + A.5]
```

$$\mathcal{D}_{\text{had}}$$
 $(A+B) \cdot (A+C) \cdot (B+C) = (A+B) \cdot (A+C).$ 

$$\frac{1}{2} = \frac{A \cdot (B + C)}{A + (B \cdot C)} = \frac{A \cdot B + A \cdot C}{A + B \cdot C}$$

$$A + (B \cdot C) = (A+B) \cdot (A+C)$$

$$(\hat{x} + \bar{x}) = (\bar{x} + \bar{x}) (\bar{x} + \bar{y})$$

$$(\hat{x} + \bar{x}) = (\bar{x} + \bar{y}) (\bar{x} + \bar{y})$$

$$(\hat{x} + \bar{y}) = \bar{x} + \bar{y}$$

$$\rightarrow$$
  $AB + AC = (A+B) (A+C).$ 

$$\Rightarrow \sqrt{x\cdot y + y\cdot z} = (x+y) (y+z).$$

De Morgan's Law:

@ NOR gete = Bubbled And gete A+B+C+... = A.B. - -... -> (b) MAND gerte = Bubbled OR gerte. A.B.C.D... = Ā + B + C + D + ... Shannon's Lew: -> To find Complement of a fun F'. (i) Find the Duce OF Fie. 'Fo'. (ii) Comprement all variables.

Ex-1 F = AB+BC+CA then F = A·B+B·C+c·A [JIF].

F= AB+BC+(A.

: FA (AXE). (BAR). (E+A).  $= \left( \overline{A} \overline{B} + \overline{A} \cdot \overline{C} \right) \cdot \left( \overline{C} + \overline{A} \right).$ = AB+A·E + ABE+A·E. = AB + A.E. +

i) F= (A+B). (B+C). (C+A).

(ii) 
$$\vec{F} = (\vec{A} + \vec{B}) (\vec{B} + \vec{c}) (\vec{c} + \vec{A})$$
  

$$= (\vec{B} + \vec{A}\vec{c}) \cdot (\vec{c} + \vec{A}).$$

$$= (\vec{A} + \vec{A}\vec{c}) \cdot (\vec{c} + \vec{A}).$$

Simply the tollowing boolian expression to bour literals.

① F=AC + CO+ BC+ AB. → 4 literul.

Note: Literer: vanusie (d.) Compiement of vanubles.

Eg: F(A,B,C) >> A,Ā,B,B,C,C.

F= (A+B) C + co+ AB.

F = AB. C + CD+ AB.

: F = AB+C + ED.

F=AB+ C+D

Ex-3 Determine the number of two input NAND gettes required to imprement the Pollowing:

Ans:  $\omega F = (\bar{x} + \bar{y}) (\omega + \bar{z}).$ 

F = PW. PZ

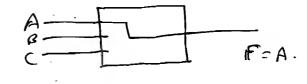
:. \$ = (@tx) · (@x2)

4 NAND gets reg.

F= = x.4 (w+2).

 $\therefore F = \frac{\overline{x \cdot y} \omega + \overline{x \cdot y \cdot z}}{\rho \omega + \rho z}$ 

(b) F= A+AB+AB(. = A + AB (1+C). = A + AB. = A (1+B)



'O' MAND gestes.

=> O NAND geste is required.

(c) n-input AND gete = ?

NAND gedes → 2ip ANO ⇒ P = A·B = 2

ZIP AND => F= ABC

4 i/P AND => F= ABCD = 6.

nilp AND =) (20-2) 20-06 2118 MANO gete rea.

Ex-& Implement Ex-or gate using minimum no. of @ NAMD gute & HOR gete.

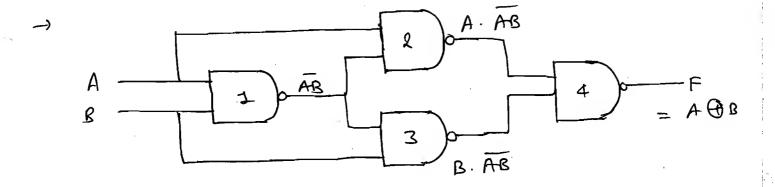
AB= A.B+ A.B

 $= \overline{A \cdot B} + \overline{A \cdot B} + \overline{A \cdot A} + \overline{B \cdot B}$ 

 $> B(\overline{A} + \overline{B}) + A(\overline{A} + \overline{B}).$ 

A. AB + B. AB.

$$\overline{F} = \frac{\overline{A \cdot AB} + B \cdot \overline{AB}}{\overline{A \cdot AB} + \overline{B \cdot \overline{AB}}}$$



$$F = A(\overline{A} + \overline{B}) + B(\overline{A} + \overline{B}).$$

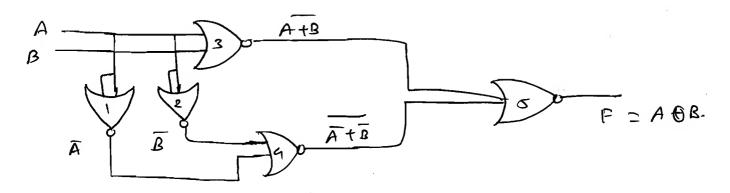
$$F = \overline{(A+B)(A+B)}$$

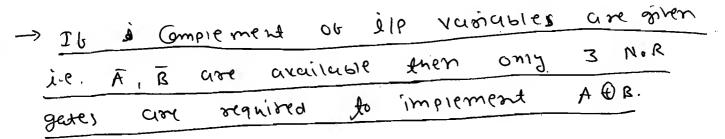
$$= \overline{\left(\overline{A} + \overline{B}\right) \left(A + B\right)}$$

$$F = \frac{\overline{\overline{A} + B}}{\overline{A} + B} + \frac{\overline{\overline{A}}}{\overline{A} + B}$$

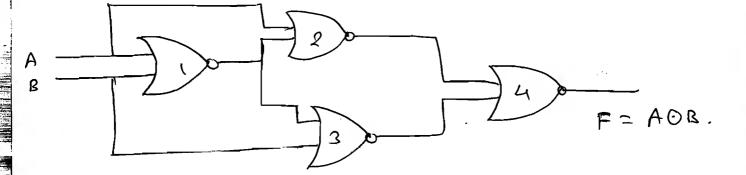
5 NOR gett.

$$A = \frac{1}{10^{\overline{A}}}$$

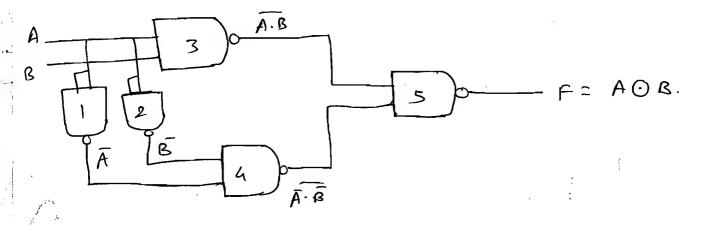




\* X-MOR using min. no. ob Mor geste:



\* X-Mor using min. no. MANO gates.



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Properties.
   Minterns, Maxterns &
    Minterns -> Stundard Product term.
                                  Sum
                                         tem.
  maxtems - Stundard
                                        Lucix Jem ? -> 8
      Minterns -> 8
                                         A + B + C
       A · B · c
mo
                                        \frac{1}{A} + \frac{1}{B} + c
       \frac{\circ}{A} \cdot \frac{\circ}{B} \cdot C
                                         A + B + c
     \frac{\mathsf{A}}{\mathsf{A}} \cdot \mathsf{B} \cdot \frac{\mathsf{C}}{\mathsf{C}}
                                   My A+B+C
     A - B.C
m_3
                                   M3 A+ B+C
     A . B . c
                                    M2 A+ B+ C.
        A . B . C
 Ms
                                         A+ B+c.
                                    MI
        A-B·C
 me
                                        0 0 C
                                     M.
         A - B · C
  Var = 1
                           and find m23 = 8, 1 M19= 8
    F ( A, B, C, D, E)
```

Ex-1 10111 Ans: M23 = A.B.CDE

1 0 0 1 1 A+B+c+o+E

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\* Properties: (1) n-var Function =) [2 minterms. Ms = mi and vice versu.  $m_i^0 = M(2^n - 1 - i).$ M3 = A+B+C M3 = M23-1-3. Sum of an minterms=1 in 5 mi=1. (b) Product ob all maxterns = 0 1.e. IT M; = 0. 0 BEL DA How many minterms are Present at ()the old ob + Ex-or gete: 26-1 = 32 no. ob AB= AB+ AB. A (BB = m, + m2 [2 out of 4 minterns]. ABBOTE AB (·) · ABBEC = mi+m2+m4+m3 [4 out of 8 minterns] n-input Ex-or gute output (ontain) = 2 : A BABADA about mintery, NOTE: Same for X-NOR.

How many booligh for cent be formed us Ex-3 using n-bootium variables! Boolium Vunable - Boolium timitims  $x = 2^{n} \text{ minterns} \quad 2x = 2^{2n}.$ 

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F(A,B)

|                  | AB | Fo         | Fi  | F2  | F3       |            | Fis       |
|------------------|----|------------|-----|-----|----------|------------|-----------|
| mo <             | 00 | 0          | 0   | 0   | 0        |            | 1         |
| $m_i \leftarrow$ |    | 0          | 0   | 0   | <b>Ø</b> |            | 1         |
| Mr ←             | _  | 0          | 0   | 1   | 1        |            | 1         |
| m3 x             | 11 | 0          | ١   | 0   | 1        |            |           |
| : .              |    | ١ở         | 1   |     | . [      |            | 1         |
| • .              | C  | )<br>NW(1) | Ano | Y   |          | -> Lenulla | Identity. |
|                  |    |            |     | Inh | 15iti    | ፅ <b>ጉ</b> |           |
|                  |    |            | (   | AB  | ()       |            |           |

torms ob Boolean Functions:

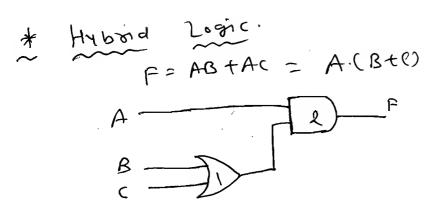
- a) Sum of Products (SOP) form > DNF
  - Sym (POS) togim. -> CHF b) froduct ob
- a) Canonical (0%) Stundard Sop form (sum of minterns, 2) b) Camonica (of) Stundard pos form, (product of max terms)

- DNF = Disjunctive Normal bostom ( NF = Conjunctive normal born.

DCF = Bisiun(fire amonical form

> CCF = Conjuctive Canonical form.

 $Ex-1 F(A_1B_1(C_0)) = \overline{A} + \overline{A}(\overline{O} + \overline{B}(C_0)) + \overline{A}(\overline{O} + \overline{B}(C_0))$ 500 to 8m. Csum of minterns from F(A, B, C, O) = AB+ AB + ABC + ABC -+ Ans:  $F(A_1B_1C_1D) = \overline{A} + \overline{ACD} + \overline{BC}$ A- C D mo 6 0000 0000 7010 Jm1. 000100 61 01 1 Jm1 0611 0 1 : P(A(B)C(0)= Em(0)(1,---7,10,11) & Cun SOP form. : F(A,B,(,0)= TTM (8,9,12,13,14,15) & Can Pos togm. Convert F(A,B,C) = A-B + A-C into amonical pos term (product of maxterns) Ans: PEARCI = A.B. + A.B. Ma 000 1 10 1 Ma : SOP Comsor Pos



The advantages of two level logic is

the propogertion for all the input Variables

Same.

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(3)

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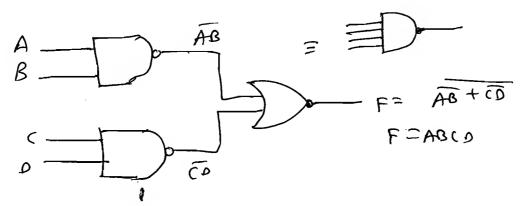
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Types ob Two Level Lugic:

- (2) Non-Degenerative.
  - 1 Degene outive.
  - => There are only one logical operation in of them it is called Degenerative type.

e.g. MAND-MOR Logic



The cidvantages of Degenerative born is

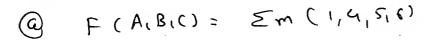
the training of the gate is increase.

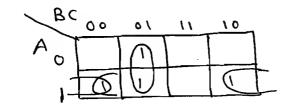
\* Karnaugh Maps (Veitch Diagram). 49 K-Map: \* 3- Vanable F(A,B,c) ( goup ob 8 adi mintems). octet (gover ob a adi minderns). ( Gromp ob 2 adj minterns. a: How many possible was to get oned or mintems. Ans: 6. \* 4- Variuble possible ands => 24 CD 01, 97 00 possible octets => 8. AB 3 PUIT => 32 00 Possible 7 (0,2,8,10) =) Onad 0 | 13 15 11 9 11 8 10 Rows Colums

Colums Rows 1,2 1,2 1,3 2,3 2,3 2,3 3,4 4,1

)

Ex-1 Simply the following expression using maping





(b) F(A,B,C,D) = Em(O,1,2,4,5,8,9,10,12,14,15).

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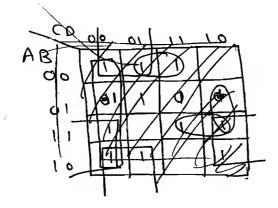
( )

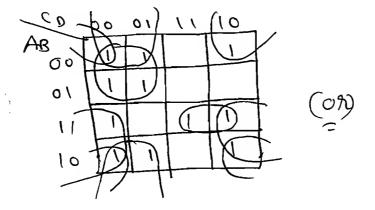
<u>C</u>

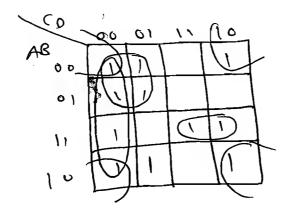
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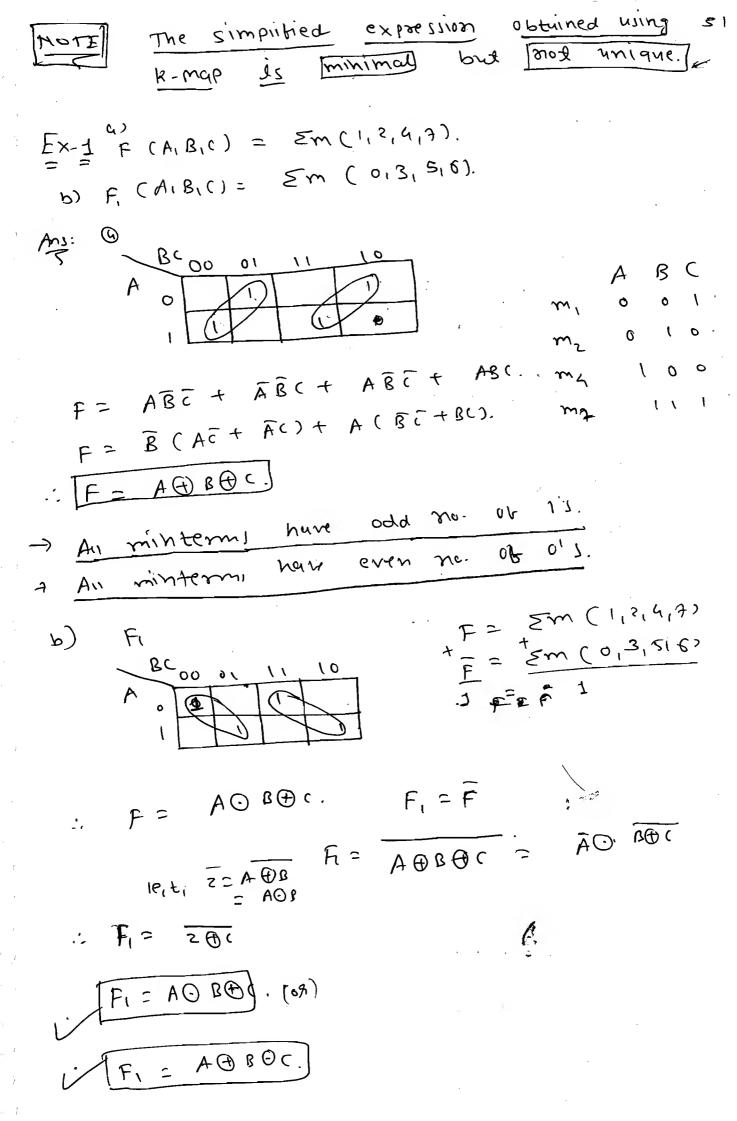
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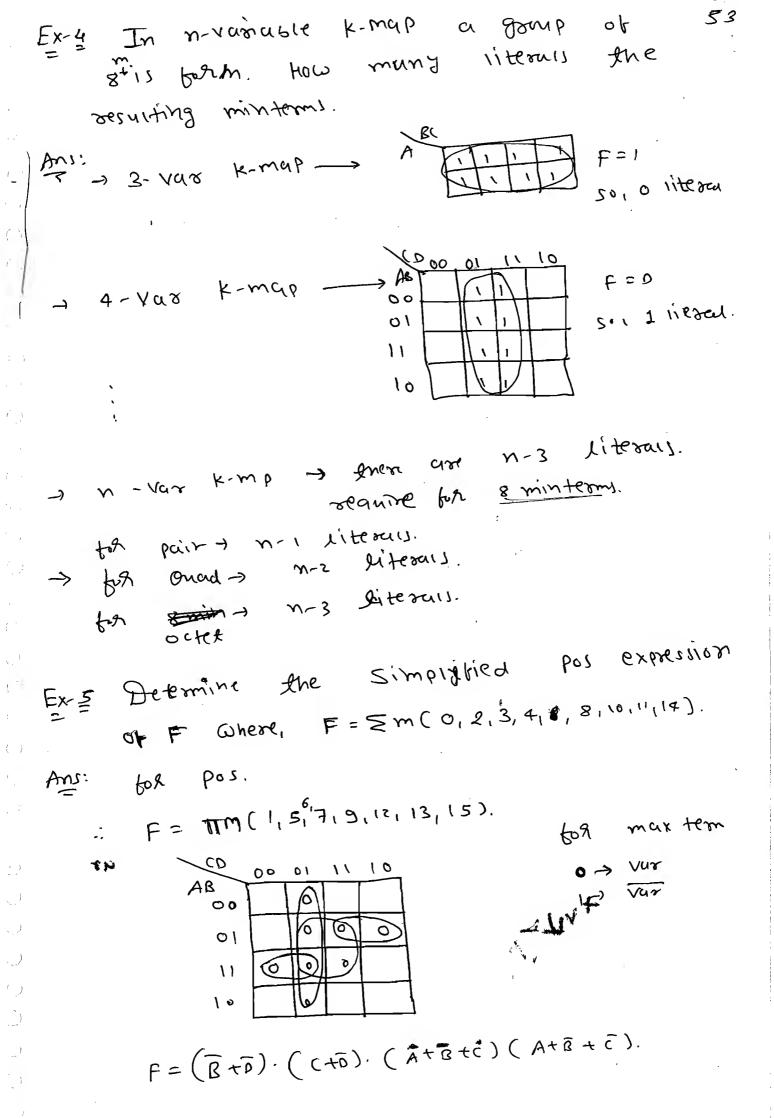








and have 26201 doesn't 000 Winferm, 4 even no. of 1's. Sym of mintern Represent F = ABBBCBD in Ex- 2 (Comonica sol form). F= A & B @ COD. OF C OF D. 0 0 0 9 0 O 01 11 G 0 ANS: 8  $\langle \rangle$ O Ç ()f = zm(1,2,4,7,8,1,(3,14). 0 above minterns have no-ob ones. Simplify the following frames: po €ma (0,3,5,6,9,10,12,15). 00 01 11 10 minterms antain even NO. 26801 X-NOR Jake.
AOBOCOD.



\* Implicant:

-> (i) Prime Implicant &

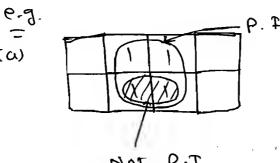
(ii) Essential implicant

Implicant:

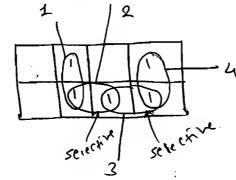
→ it is the <u>Set of all</u> adjectent mintermy

\* Poime implicant:

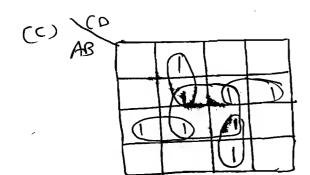
- It is an implicant which is not a subject of another implicant.



NOT P.J.



poime impliants.



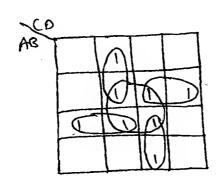
(d)

All are prime implicants.

| * | Essential | Poime | impricants: |
|---|-----------|-------|-------------|
|   |           |       |             |

The is a poime implicant which contains afterest 1 minterns which is not covered by another prime implicant.

e.g.



essential prime and remaining are essential prime impricant and essential prime impriant.

\* Mon-Essential Prime Implicants:

\* Mon- Essential Prime

D Redundant P.I (RPI).

It is a non-essential prime implicant whose minterns are covered by all essential P.I.

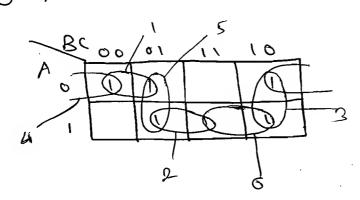
2) Selective Prime implicant:

Tt is a non-essential poime implicant anose minterns are Covered by at realst one non-essential P.I.

\* Minima Expression = EpI's + (optional) SPI

Ex-1 Determine the essential P.I. and minimal expression for the tomowing the

Ans: (1) F(A,B,C) = Em (0,1,2,5,6,7).



SPI, 1 → 0 '0' 0' 0' 0 SbI, 1 → 0 '0' 0' 0' 0

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(a) F(A,B,C,0) = Em (0) 1, 4, 5, 6, 8, 9, 10, 12, 14, 15)...

AB

OO

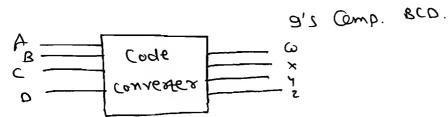
11

OO

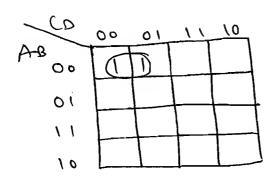
FPIS= 5, an

A Don't Care Condition: -> In a digited System took a mon-occurring 11P, the OIP Com be consider ay either 0 (09) 1 during its simplification and it is caused the doorst care andition. · FCA(B)= Em(0,2) + d(2). oigital 01P 10

BCD Code Ex-1 Design Bro to 9's Comp. of Converter.



(i) for w:



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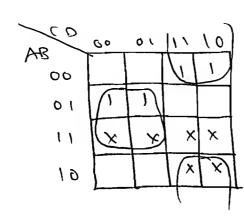
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 $(\dot{})$ 

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$$X = \Sigma m (5'3'4'2) + q (m1'-12)$$

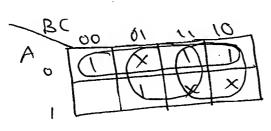


(iii) Y = Cdisect from T.T. (iv)  $z = \overline{D}$ disect from T-T

The purpose of minimization is to orduce the number of ligit gates and no ob inputs.

 $Ex_{-1}(i)F_{i}(A_{i}B_{i}C) = \sum_{i} m(o_{1}2_{i}3_{i}5_{i}) + d(l_{i}G_{i}A_{i}).$   $(i)f_{i}(A_{i}B_{i}C) = \sum_{i} m(o_{1}l_{i}2_{i}3_{i}G_{i}) + d(l_{i}G_{i}A_{i}).$   $Find F_{3} = F_{i}F_{2}.$   $F_{4} = F_{i}F_{2}.$ 

Ans: (1) Em (0,0,23,5) +d(1,6,7)



F1 = A + C + B.

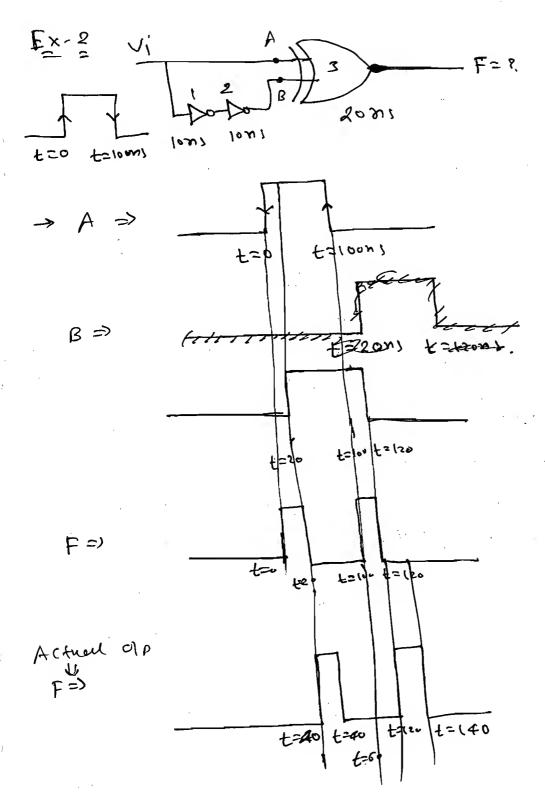
(ii) Em(011,2,3,6) + d(4,517).

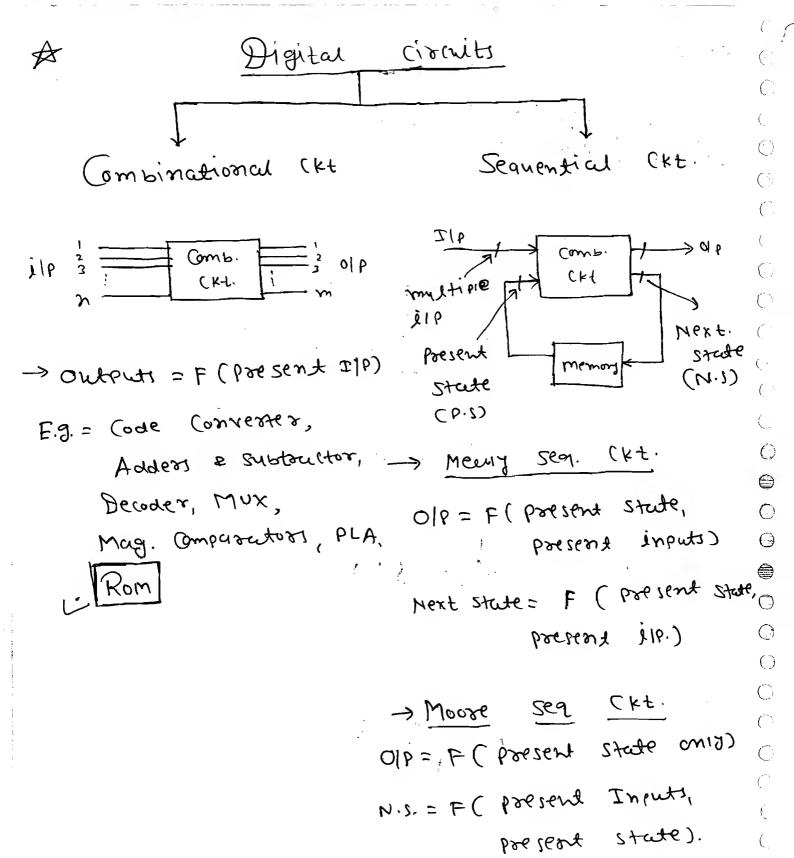
| BO  | 00 | 01 | 11,      | 10 | 1 |
|-----|----|----|----------|----|---|
| MOT | 1  | ,  |          | 1  |   |
| ļ   | *  | *  | <u>x</u> | 1  | 7 |

F2=1.

$$F_{4} = F_{1} + F_{2} = 1 + (A+C) = 1$$
  
 $F_{4} = F_{1} - F_{2} = F_{1} = A+C = 1$ 

(Oh) 0.000 1+ 0= 1 1-9=9 b = b + 0 J. d = , d. b = b x b  $F_3 = F_1 + F_2 = \sum_{i=1}^{n} (0, 1, 2, 3, 5, 6) + ol(4, 7)$ F4= F1-F2= Em ( \$4,2,3)+ d(1,6,7,5). 0 Ex-2 F, (A, B, C) = Em (0, 3, 5,6) +d(2,4,7). F2 ( A,B,C) = Em (1,2,3,6) + d (0,5,7). F3= F1+f2= Em(0,1,2,3,5,6) +d(24,3). Fa= F. F2= Em (316)+ d(0,2,517). Ex-3 Determine the Gavetorm of the olp of the following lugic Ckt. pro-delaz= 10m) F=8 20ms. Actual OIP. AS 0 1 1007 ()£ => BOD 30 M) 20ms 0 t=Lons ( ,

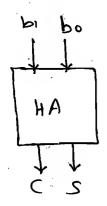


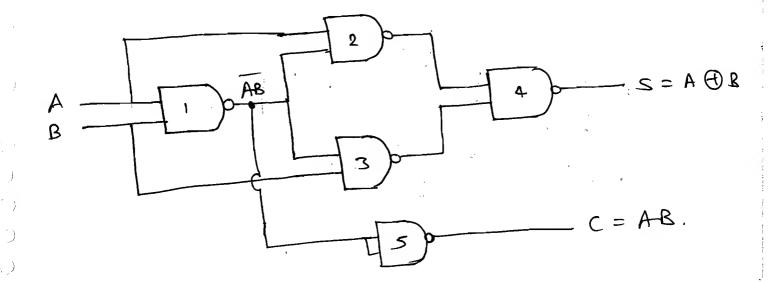


E.g. Shift register,
Counters, carculators,
Mr, PC.

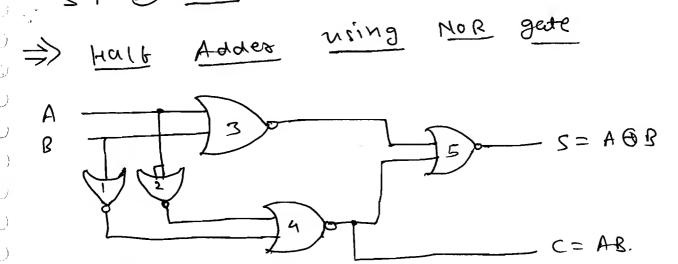
\* Avithmetic Combinational Ckt.

## (1) Hait Adder:



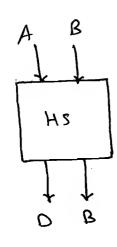


So, 5 MAND geste required



(\$) So, MOR Defe regulred

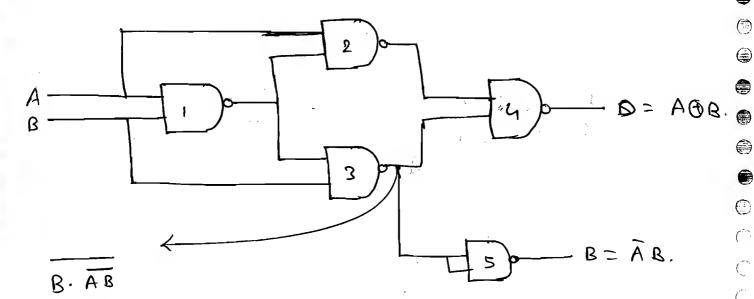
Subtractor: (2) Hait



| A | B | 0  | ß |
|---|---|----|---|
| 0 | 0 | 0  | 0 |
| 0 | 1 | 1  | 1 |
| Ţ | ٥ | 1  | 0 |
| t | 1 | 10 | 0 |
|   | , |    |   |

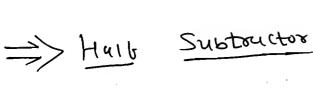
$$D = A \oplus B$$

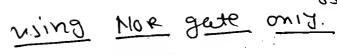
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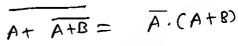


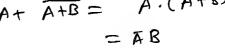
$$=\overline{B}+AB$$

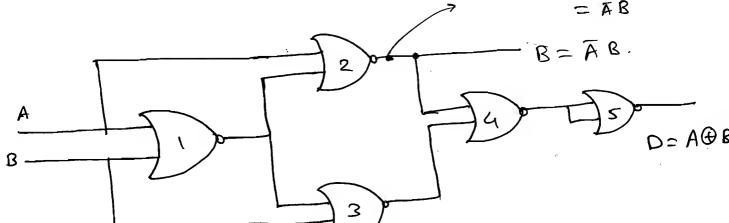
$$= A + \overline{g} = \overline{A \cdot R}$$

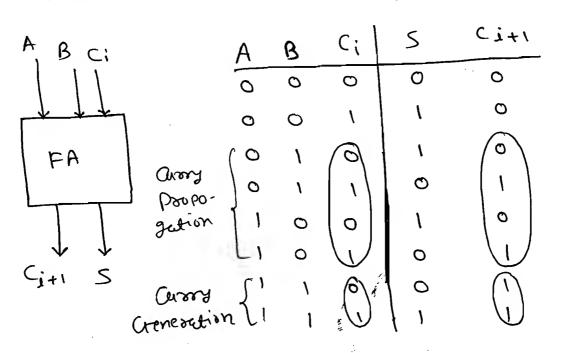


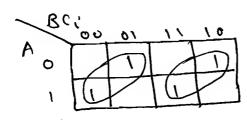












$$S = A \oplus R \oplus C$$
; (ob)  $A \oplus B \oplus C$ ;

$$C_{i+1} = \sum_{i=1}^{n} (3, 5, 6, 7)$$

$$= \overline{ABC_i} + \overline{ABC_i} + \overline{ABC_i}$$

$$= C_i (\overline{AB+AB}) + \overline{AB}.$$

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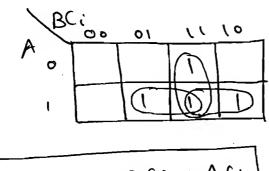
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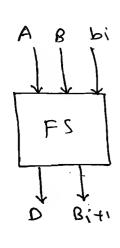
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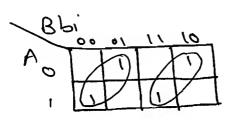
NOTE: Full adder

- (i) Reanire 9 NAND geste
- (ii) Require 12 NOR gate.



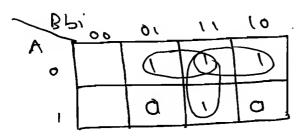
| A  | B  | bi       | 0        | bi+1     |  |
|----|----|----------|----------|----------|--|
| 0  | 0  | a        | 0        | 0        |  |
| 0  | 0  | 1        | 1        | <u> </u> |  |
| 0  | 1_ | 0        | <u>'</u> |          |  |
| 0  | l  | 1        | 0        |          |  |
| (  | 0  | <b>*</b> | 1        | 0        |  |
| `, | 0  | 1        | 0        | 0        |  |
| ۸  | 1  | 0        | 0        | 0        |  |
| 1  | 1  | \        |          | . 3      |  |
| ı  |    |          | 1        |          |  |

-> D (A,B,bi) = Em(1,2,4,3).



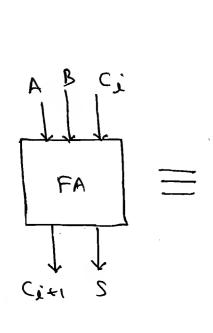
→ bi (A, B, bi) = \le m (1, 2, 3, 7).

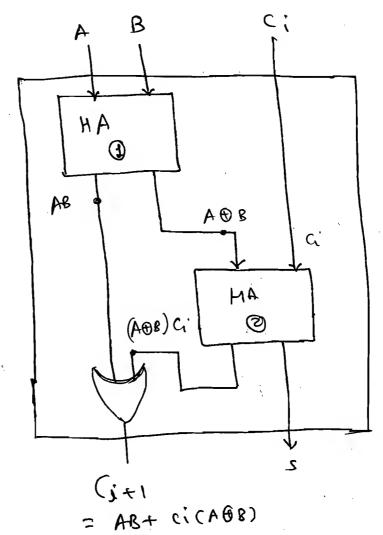
bit(=  $m_1 + m_2 + m_3 + m_4$ )  $= \overline{ABbi} + \overline{ABbi} + \overline{ABbi} + \overline{ABbi}$   $= \overline{Bbi} (\overline{AB} + \overline{AB}) + \overline{AB}.$   $= \overline{Bbi} (\overline{AOB}) + \overline{AB}.$ 



MOTE: (i) Required 9 NAMO gerte.

(ii) Required 12 MOR gerte.





+ 1 OR geste hail adder 2 adder = 1 Fun

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How many HA required to implement the finawing by.s.

FI = AC + ABC + BC.

Fz= A + B + C.

F3 = ABC + ABC.

Ans: (i) Fr = Ac+ ABC+ BC.

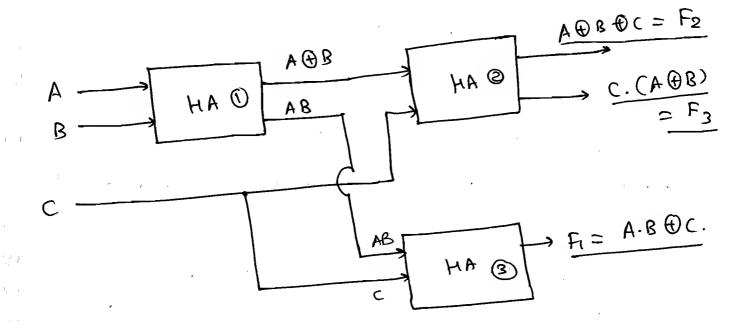
= AB.C + ABC

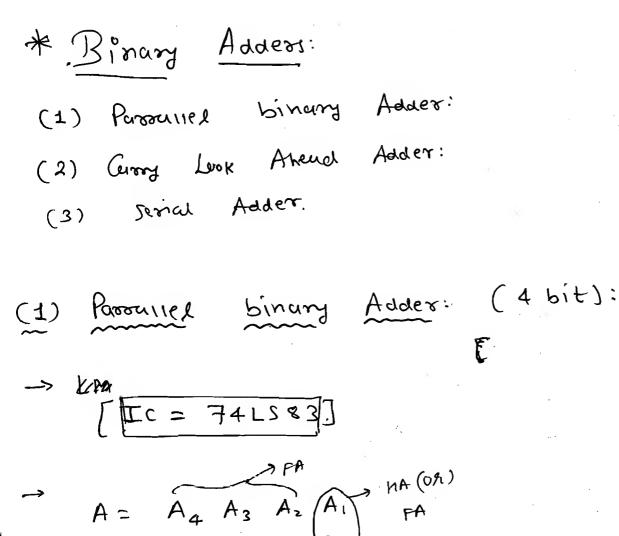
Q (MAB) · C X = AB.

= x.c +x x E

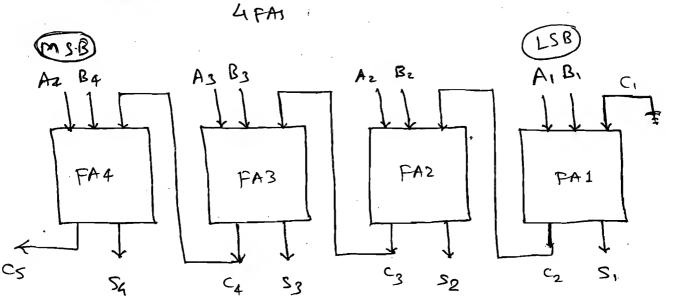
F= A.BOC ->

FROM (11) F2 = A &B &C. (iii)  $F_3 = (\overline{A}B + A\overline{B}) = (.(A \oplus B))$ 





(Oh) 3 FA + 1 HA



to imprement 4-bit 1181 adder HA. required

HA & 7 Wis. OR gette 3

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In a 4 bit paranel binary adder FA takes 32 ms to produce the sum and 14 ms to produce the away. Determine (i) Time required ton addition.

(ii) the adition rate of the adder.

Ans: a)

Time required for Addition in 
$$N-Bit$$

paraula adder =  $T = (N-1)t_c + max(t_s, t_c)$ .

$$= 42 + 32$$

Addition Rute = 
$$\frac{1}{74 \times 10^9}$$
 Hz.

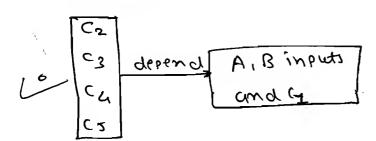
-> This can be used upto 4 bit.

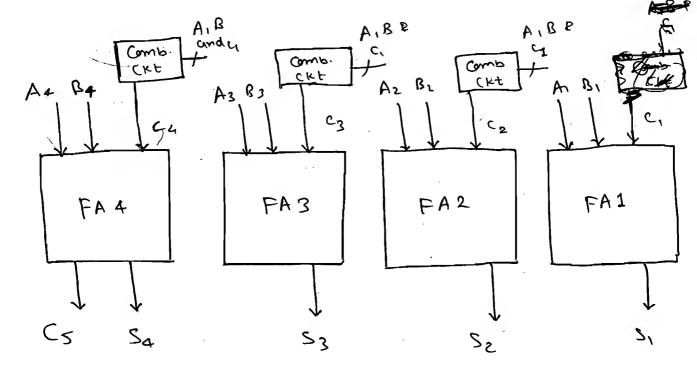
-> Disadvantages:

-> ay the Size of the Adder increuses the Speed operation decreuses as the army has to propogate through at the FA, to overcome this we use covery Look ahead

Adder.

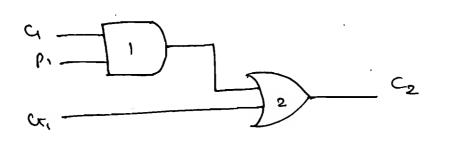
-> & Principie:

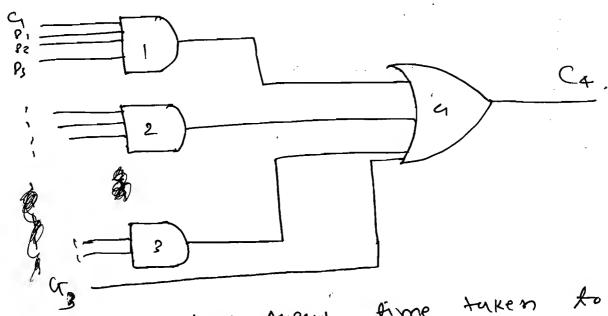




$$\rightarrow \quad C_4 = \quad C_3 p_3 + \quad C_3$$

\*





Look-Aneud firme taken to In am generate the carries C2, C3, C4 is same 2 level Logic. as they are imprimented by

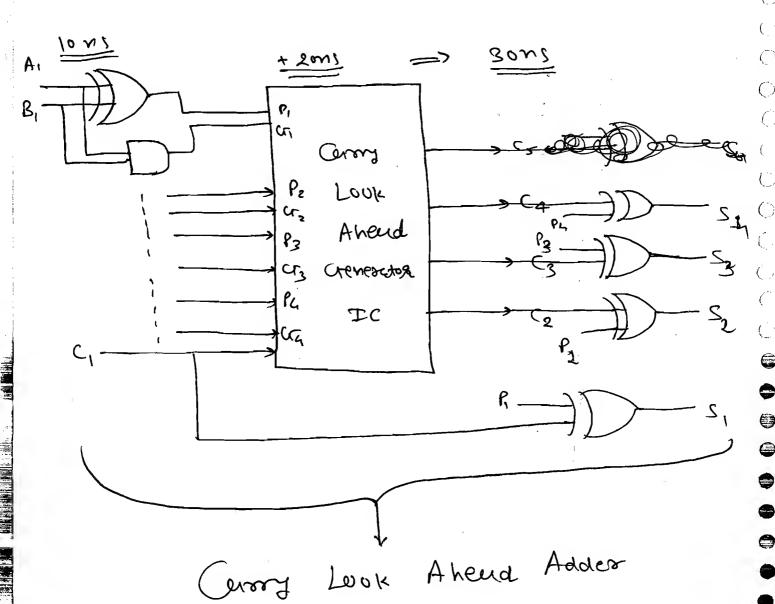
#### \* Advantage:

-> Its speed of operation is very high and doesn't depend on the size of the adder.

Disadrantuol:

-> It has more hardware Complexity. To Overcome this we use any look ahead generator Ic.





S; = A; ⊕ B; ⊕ c;

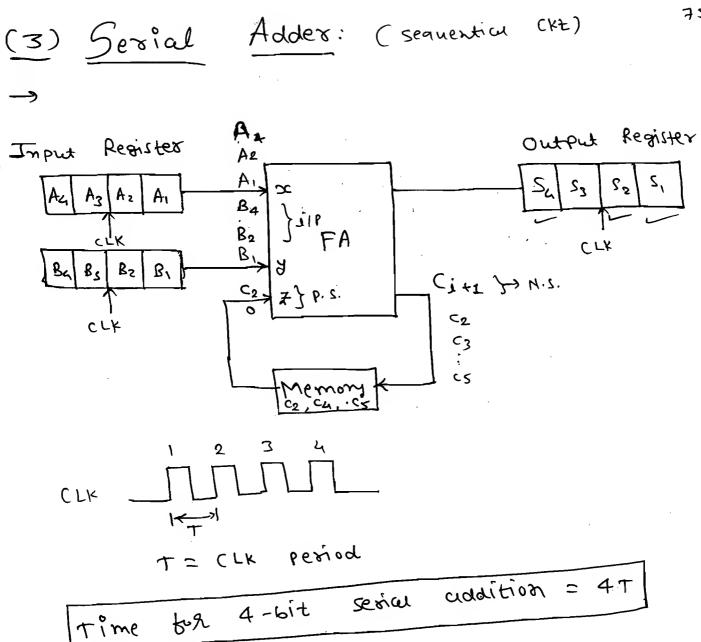
s; = β; € c;

Si= Pi @G

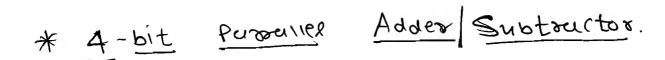
Sz= Pz &Cz

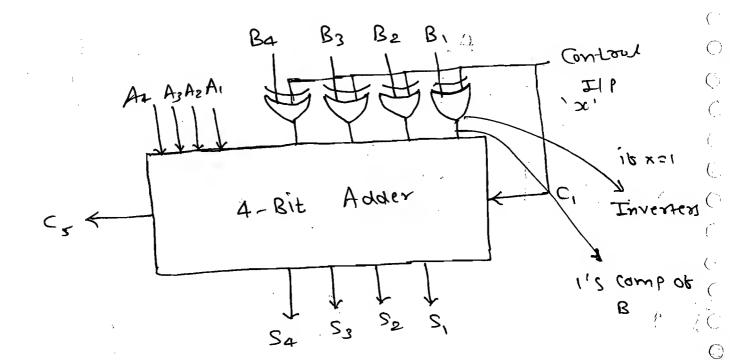
S3= P3 (C3

Su= Pa & Ca.



Time





(1) It 
$$x=1$$
  $\Rightarrow$  Ex-or gate  $\Rightarrow$  Invertext
$$\Rightarrow A + i's \quad (amp \ ob \ B)$$

$$\Rightarrow A + (2's) \quad (amp \ ob \ B)$$

$$\Rightarrow A - B \Rightarrow Binary \quad Subtauction$$
(2) It  $x=0$   $\Rightarrow$  Ex-or gate  $\Rightarrow$  Bubber

Ex-1 Determine the th ob the above 77 circuit it the inputs are as given below:

@ x=1; A = Ex-3 code; B=0011 => Fun(tion=9

 $\Rightarrow A - B = Ex - 3 - 0011$  = Ex - 3 + (1100) + 1

= Bco Code.

Ex-3 to BCD (ode Consterter.

1 1 1 | Ex-3 > 0100 -> BCD

(b) x=1 , A=1001; B=BCD => Functions!

Ans: A = 1001. | let, B = B(D of 3

: A A-B= 1001 + 1100

= 6,0 which is 9's comp. of 310

" So, BCD to g's Comp. of BCD.

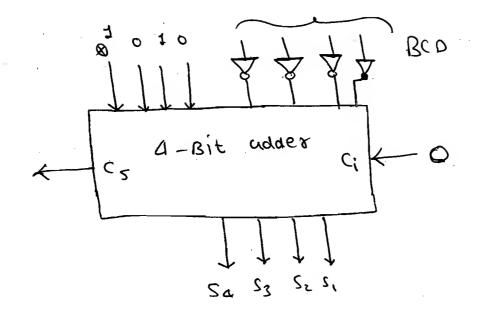
At iscomp of B+ C,=1.

= A + (2's (comp of B).

= A- BCP.

= 810-BCD

= 915 complement of BCD.



(C)

-> 9's comprement of (kt.

NOTE: The above 9's Complement (kt Can be Converted to a to's Complement either by (hoosing C1=1 (of) by choosing A value Cay A=1011

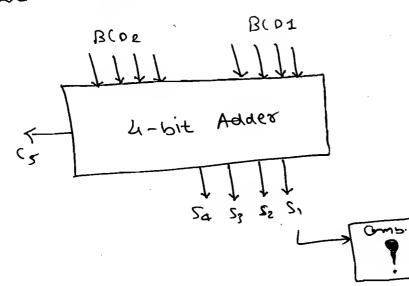
**(** 

4

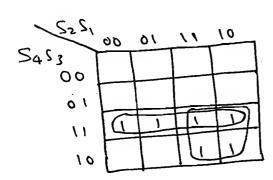
0

<u>C</u>

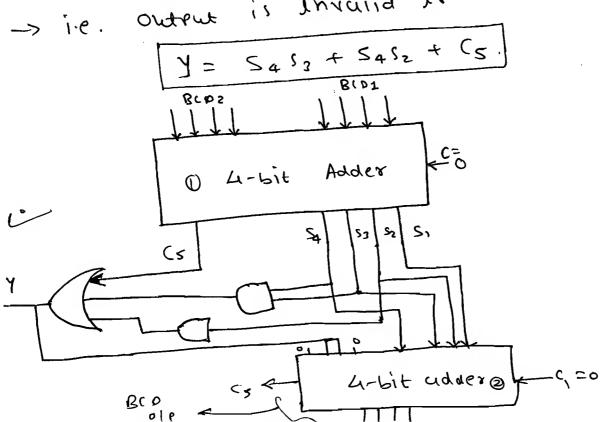
\* BCD Agges

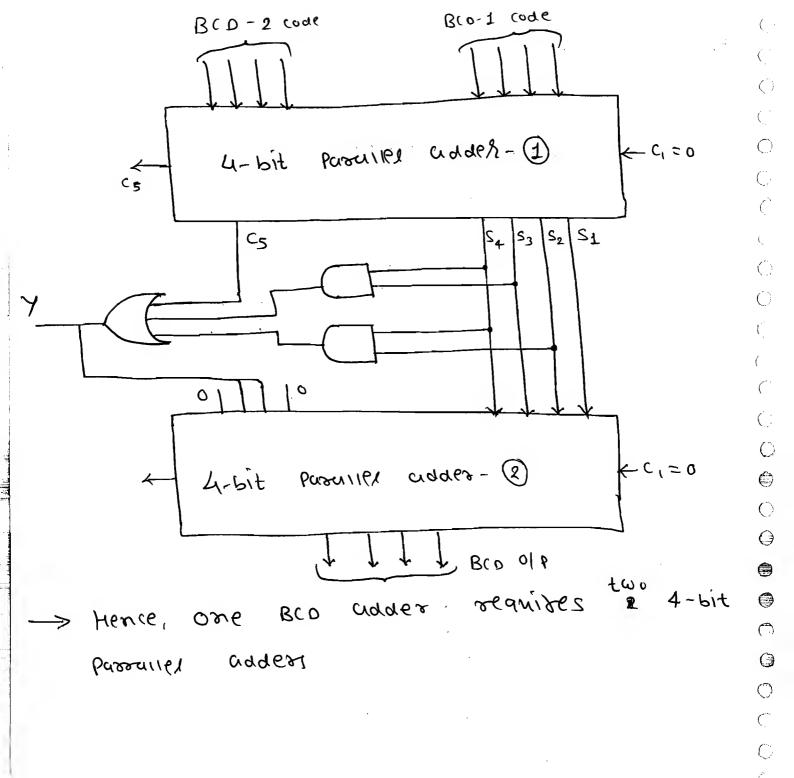


if. BCD \* Output is invarid S453525,79 (02) C5=1.



-> i.e. output is invalid it





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<u>(</u>)

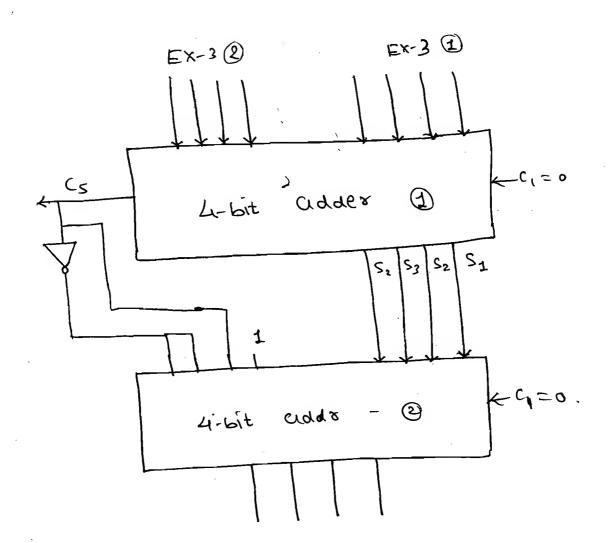
\* Ex-3 Adder

(1) If 
$$C_5 = 1 \implies Add = 0011$$

(2) It 
$$C_5 = 0 \Rightarrow$$
 Subtract 0011

= And 215 Comp of 0011

= Add 1101



\* 2-Bit Magnitude Comparator:

The touth tuble of n bit magnistude Compusator is not preferred for the design of the no. of rows or in the tuble of 2.

They A>B?

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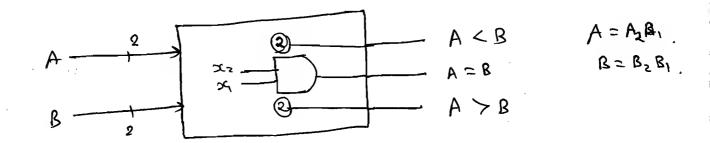
Ans:  $A_2 A_1$   $B_2 B_1$   $0 0 \longrightarrow \mathfrak{D}$   $10 \qquad 00) \longrightarrow \mathfrak{D}$   $11 \qquad 00) \longrightarrow \mathfrak{D}$ 

50, 6 possibility that A>B.

 $A_1 \longrightarrow X_1 = J \quad \text{ib} \quad A_1 = B_1 \Rightarrow x_2 = 1$   $B_1 \longrightarrow X_2 = J \quad \text{ib} \quad A_2 = B_1 \Rightarrow x_2 = 1$ 

 $A_2 \longrightarrow X_2 = 1 \quad \text{if} \quad A_2 = B_2 = 1$   $B_2 \longrightarrow X_2 = 1$ 

 $0 \quad A=B \quad \text{it} \qquad A_2=B_2 \quad \text{and} \quad \text{assumb.} \quad A_1=B_1 \quad \text{83}$   $i\cdot e \quad A=B \quad \text{it} \qquad x_2=1 \quad \text{and} \quad x_1=1.$   $i\cdot e \quad A=B \quad \text{it} \qquad x_1\cdot x_2=1.$ 



(2) 
$$A>B$$
 it  $A_2>B_2$  (or)  $A_2=B_2$  and  $A_1>B_1$ .  
i.e.  $A>B$  it  $A_2B_2+x_2\cdot A_1B_1=1$ —(9)

Checker

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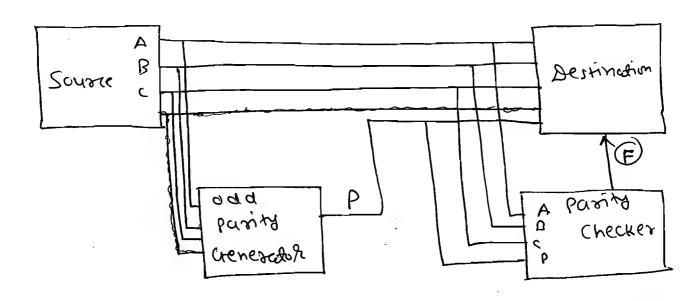
()

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0

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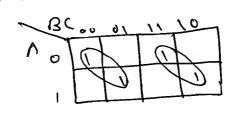
p is choosen so that AiBicip -> odd party.

F=1 it even parity F=0 it odd punty occur tot A, B, C, P.

> odd party generatur:

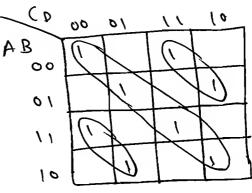
| A | B   | C | P   |
|---|-----|---|-----|
| 0 | 0   | 0 | 1   |
| 0 | 0   | 1 | 0   |
| 0 | ١   | 0 | 0   |
| 0 | Į   | 1 | 1 , |
| ţ | 0   | 6 | 0   |
| Ţ | 0   | 1 | 1   |
| 1 | 1   | 0 | 1   |
| 1 | . ( | 1 | 10  |

P(A,B,C) = Em (0,3,5,6)



PZ A & BOC (oh) P = AO + C.

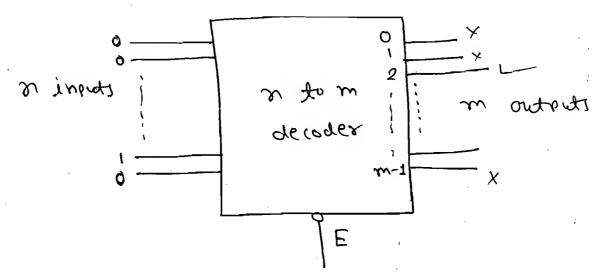
| AIB   | C P        | F   | F= &m (A, B, (, P)     |
|-------|------------|-----|------------------------|
| ,00   | 0 0        | ١   |                        |
| .0 0. | 0 /        | 0   | = Em (0, 3, 5, 6,9, 10 |
| .00,  | 0          | 0   | (0 00 01 11 10         |
|       | \ \        | \ \ | AB TOT TO              |
| 0 1   | 0 0        | 0   | 00                     |
| ·e    | <b>0</b> \ | ١.  | 01                     |
| 0 1   | ۱ ٥        | 1   | 11 1                   |
| 0 1   | ١ ١        | 0   | 10/10/10               |
| Φ 0 ( | 0 0        | 0   |                        |
| φο    | 0 /        | 1   | * Au minterms          |
| Φ 0   | 1 0        | ,   | Eren No of             |
| Φ ο   | \ \        | 0   |                        |
| Φ 1   | 0 0        |     | =) F= AOBOCOP          |
| φ 1   | 0 \        | 10  |                        |
|       | `          |     | N. P.                  |
| • '   | 1 0        | 1   |                        |
| d 1   | 4 1        | 1 1 | ·                      |



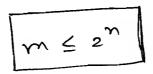
have 0'5.

## \* Decoder:

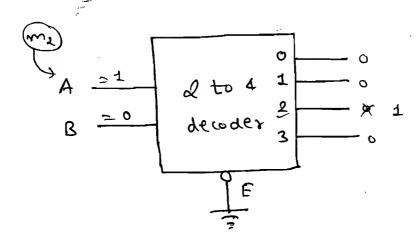
- → It converts the binary intermations
  on ilp lines to one of many olp
  lines.
- -> n to m decoder = (1 out of m decoder).

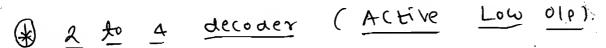


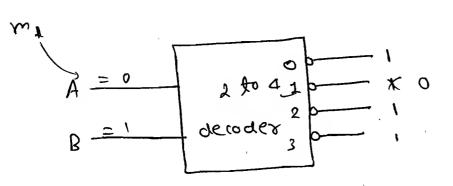
E=0 => Becoder is encubied



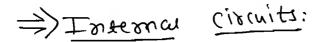
\* 2 to 4 decoder (Active high Olp).

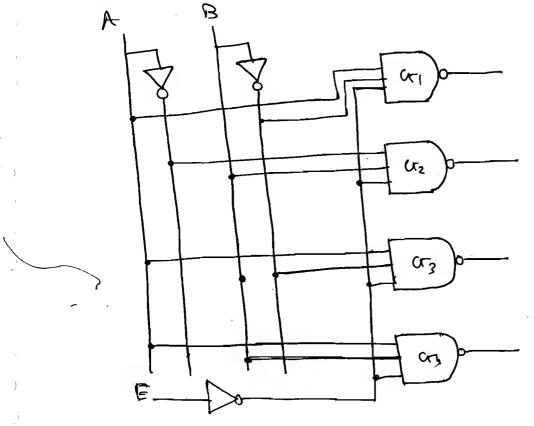






Most widery used in Practice because it generate Less noise Compure to Active High Decoder

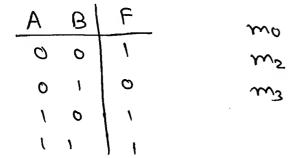


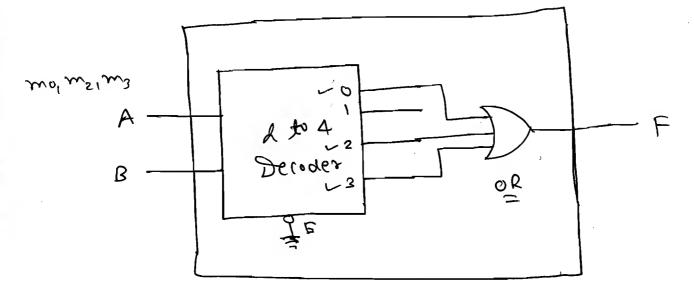


\* Decoders => AND, NAND gestes. Ex-1 Implement  $F(A_1B) = Em(0, 2,3)$ . using a decoder © with active high olps.

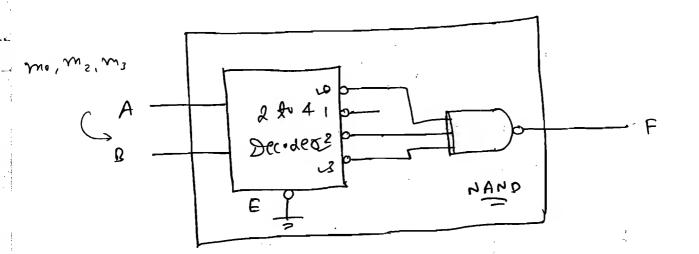
(B) with active Low olps.

Ans: @ with active high olp.





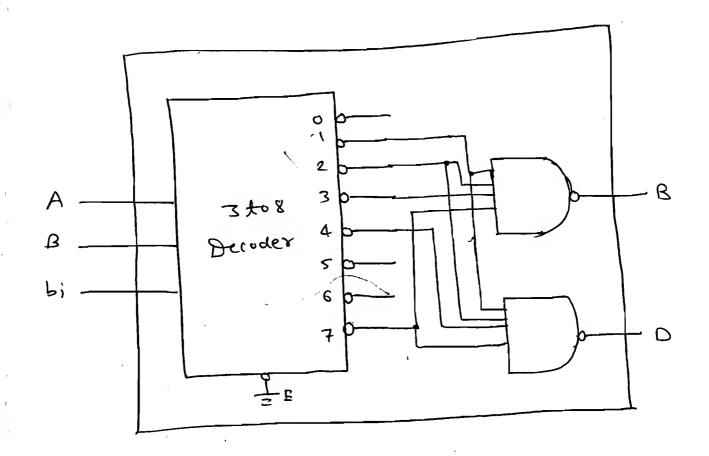
(b) with active Low OIP.



Ex- ? Imprement a buil Subtractor using a decoder with active Low outputs.

Ans:

D (A,B, bi) = 
$$\sum m(1,2,4,7)$$
.  
B(A,B, bi) =  $\sum m(1,2,3,7)$ .



Ex3 How many 2 to 4 decoder required to construct of 1 out of 32 decodoer.

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(E)

 $\left(\frac{\lambda}{2}\right)$ 

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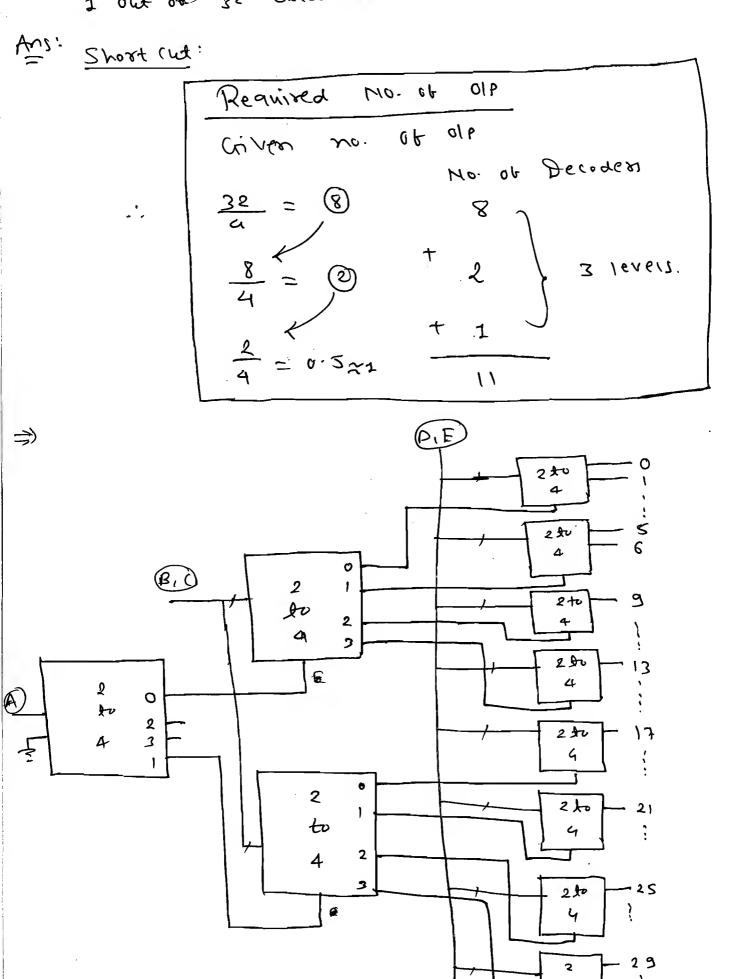
( <u>:</u>

()

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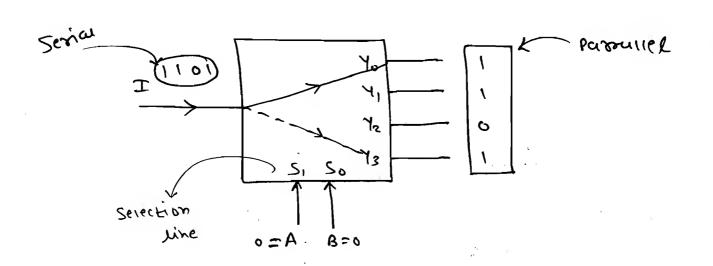
to

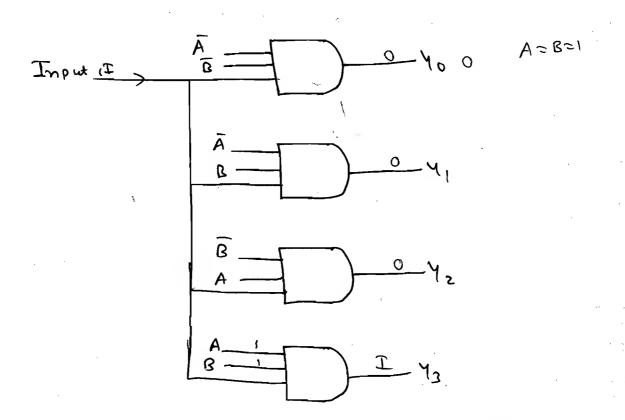
32



\* Demuitipiexel (one to many (kts, serial to granies converter)

1: 4 Demux





-> A Demux is similar to a decoder.

7 A 1:4 Demux is converted to a 2 to 4

Decoder by making two changes.

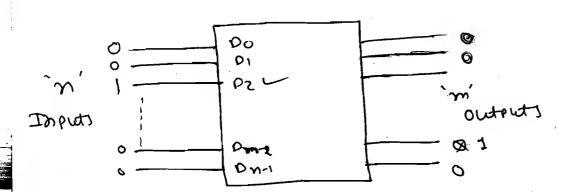
(1) selection of Demux are converted to the ilps of 2 to 4 decoder.

treested 22 工 enput demux (2) The 2 to 4 decoder enable 06 high active

0

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En coder:



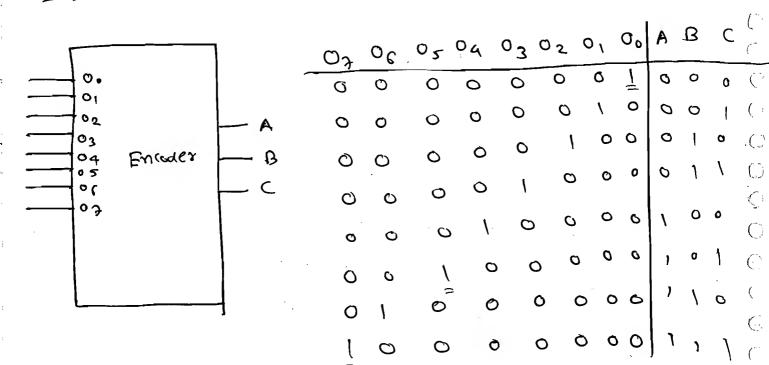
Output Code seree ted Input 000....01

It D,=1

000 --- 10. PX=1 It

\* Coding an not be performed 0,=1,0221 Ik

Design octal to Binary encoder. Ex-3

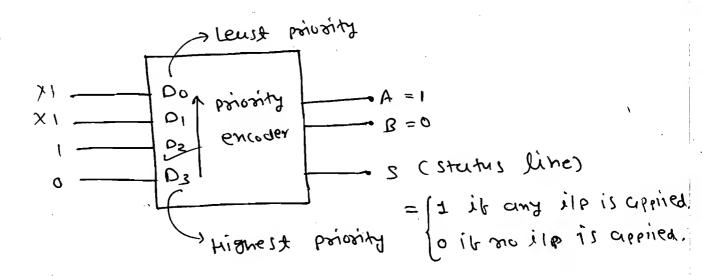


#### MOTE:

> The encoder borrows the OR Logic.

The limitation of encoder is it can't performed the coding it more than I imput is active simultaneously. To overcome this, are use priority encoder.

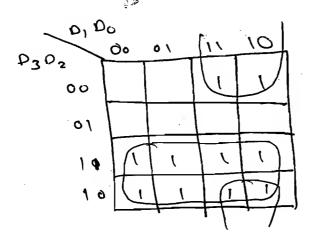
# \* Priority Encoder:



| ) ⇒> D <sub>2</sub> | Dz   | D,             | Do | A | B     | 5   |
|---------------------|------|----------------|----|---|-------|-----|
| mo                  | 0    | 0              | 0  | Ø | 0     | 0   |
| m <sub>1</sub> 0    | 0    | 0              | 1  | 0 | 0     | 1   |
| mz, ms              | 0    | 1              | ×  | 0 | 1     | 1   |
| m4 tom260           | 1    | ×              | ×  | 1 | 0     | 1   |
| mg tomis            | ×    | ×              | ×  | 1 | 1     | 1 1 |
| cha o               | 5 51 | O <sub>5</sub> |    | • | . 3.0 |     |

(b) Priority encoder ruble.

-> B( D3, D2, D, D, ) = Em(2,3, \$78, 8,3,10,--15)



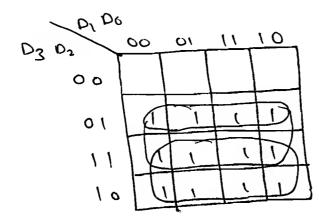
0

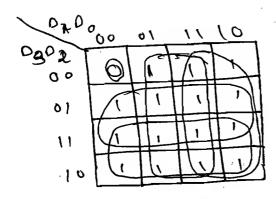
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$$S = D_3 + D_2 + D_1 + D_0$$

$$S = D_3 + D_2 + P_1 + D_0$$

### \* Multiple xer:

\*

(Many to one circuit,
paranel to serial converter).

4:1 MUX.

$$T_{s}$$
 $T_{l}$ 
 $S_{l}$ 
 $S$ 

\* F.g.: Given  $I_0 = I_1 = 1$ ;  $I_2 = I_3 = 0$ .

F= mo-1 + m, 1 + 0 to.

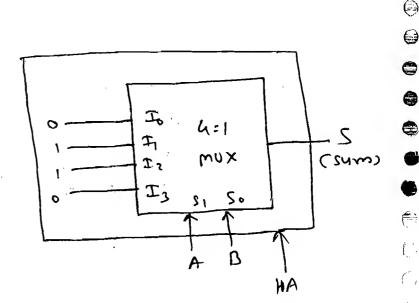
: F= mo+m,

: F= Em (0,1).

Ex-1 Implement the Sum of p of hait
Adder using 4:1 MUX.

Ans:

Scarbie  $T_1 = T_2 = 1$  &

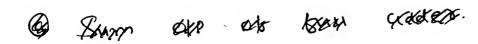


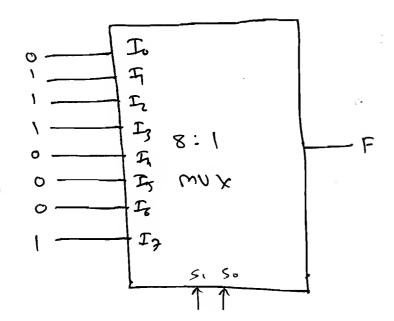
( ;

( )

Ex-2 which of the following is implemented by the following mux.

- @ Sum output ok Fuii adder.
- (b) Carry out put of full adder.
- (c) Difference output of Fun Subtouctor.
- Va Borrow output Ob Full Subtractor.





F = Em (1,2,3,7)

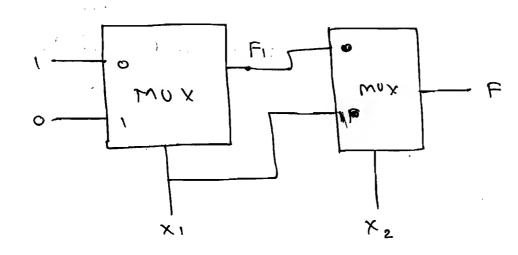
Ex-2 What use the Logic gates sepresented by the bollowing mux circuits.

F = m.c + m.c +

F=(AB+AB)C + (AB+AB)C

= AC+AC

· Ex- R gate



$$F_1 = m_0 = \overline{x_1}$$

the 04 Ex-4 Determine the output MUX. forwing

X To I, T2 De ESI By So 20 Be & Z= 0 enable By En R= ( distire.

$$F = (m_0 + m_1) \times 
+ \gamma m_2 \gamma + m_3 \overline{\gamma} 
= (\overline{S_1} \overline{S_0} + \overline{S_1} S_0) \times 
+ S_1 \overline{S_0} \gamma + S_1 S_0 \overline{\gamma} . 
= \overline{S_1} \times + S_1 \overline{S_0} \gamma + S_1 \overline{S_0} \overline{\gamma} . 
= \overline{S_1} \times + S_1 \gamma + o 
= \chi + o 
=$$

(

$$| F = x \cdot y \cdot \overline{z} |$$

$$\Rightarrow z = 0 \rightarrow \text{enuble}.$$

$$z = 0 \rightarrow \text{disuble}.$$

Ex-5 how many 4:1 mux required to constanct 128:1 mux.

Ams: Required No. of Inputs

Criven No. of Ilp

No. of: MOX  $= \frac{128}{4} = 32 \longrightarrow 32$   $\therefore \frac{32}{4} = 8 \longrightarrow 8$   $\therefore \frac{32}{4} = 2 \longrightarrow +1$   $\frac{2}{4} = 0.5 \longrightarrow +1$ 

> 2":1 MUX. (b) 2:1 MUX -No. of 2:1 mux → 4:1 mux. -> 2:1 MUX -> 8:1 MUX -> 7 → 16:1 MOX --> 12.  $\rightarrow 2^n$ ,  $mux \rightarrow 2^n-1$ . So,  $2^n-1$  mux required for  $2^n=1$  mux. Ex-5 How many 2: I MUX are req. to realize a AND geste 6 OR gute © Ex-or geste. F= AI + AI F = AB F= AB + 0. A F = 0. A+ B. A. F= A To + A To So, I, = B. B Rox F = AB.

0 0

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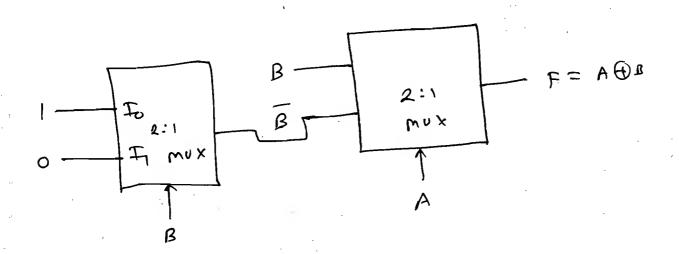
()

0

 $(\cdot)$ 

$$F = \overline{AB} + A\overline{B} = A\overline{BB}.$$

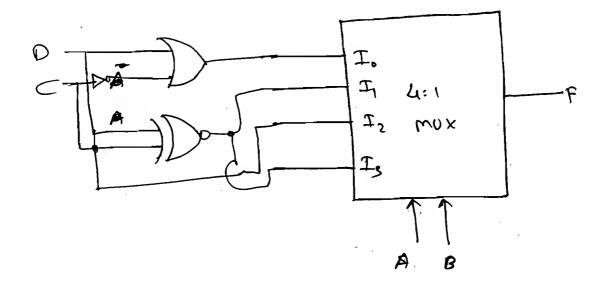
$$T_0 = \overline{AB} + A\overline{B} = A\overline{BB}.$$



Ex-6 Implement F (A, B, C, D) = Em (0, 1, 3, 5, 6, 10, 11, 6)

(3, 14) using (

Ams:



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selection like

ase

A,B

Method - 1

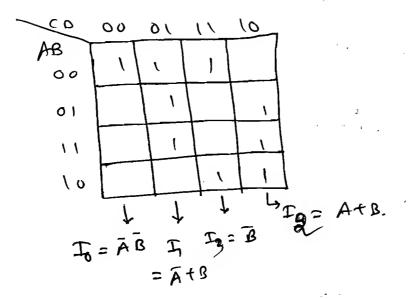
|     | AB= | 00       | ) C        | ٥ / | 11             |
|-----|-----|----------|------------|-----|----------------|
|     |     | I.       | 工          | Tz  | $\mathbb{T}_3$ |
| 00  | 0   | (e)      | 4          | . 8 | 12             |
| 0 ( | c D | 0        | <b>(5)</b> | 9   | (13)           |
| lo  | C 0 | 2        | <u>6</u>   | (0) | <u>(</u> 14)   |
| 11  | CD  | 3        | 7          |     | 15             |
| -   |     | C 5+ C 0 | COD        | C   | COD.           |
|     |     | + (0     |            |     | 1              |
|     |     | = 5 40   |            |     | 4              |

Method: 2

| C0  | Λ. | 01       |   | ١٥ |                    |
|-----|----|----------|---|----|--------------------|
| AB  | 1  | 1        | 1 | 10 | -> Io= co+co= c+0  |
| 01  |    | 1        |   | 1  | → # = ED+(0= (BD.  |
| 1 0 |    | 1        | a | 1  | → I = (0+(0= c⊕0   |
| 1 1 |    | <u> </u> | 1 | 1  | - I3 = CD + CD = C |

It

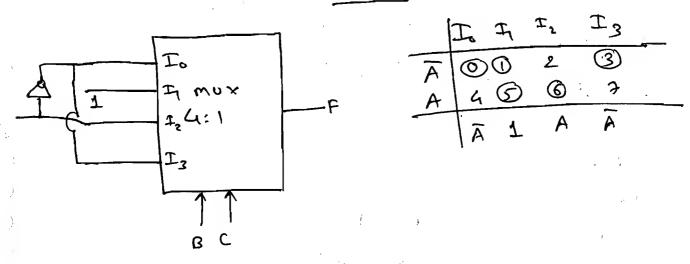
### -> Note: It CRD are selection lines



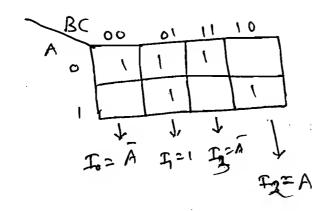
Ex-1 F(A,B,C) = Em(013,5,6) using 4:1
MUX.

Ams:

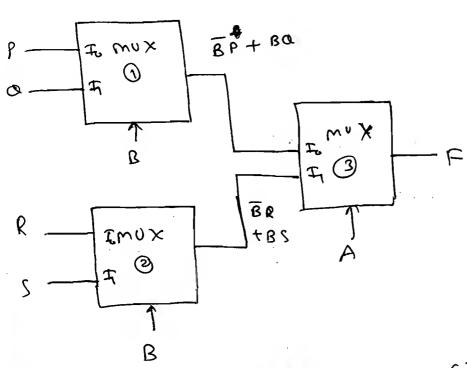
Method-I:



Method-II (K-MAP)



Ex-2 In the tollowing Mux tole, determine the A values of P,O,R,S=? Where, F(A,B,C) = EmC1,2,4,516).



$$F = \overline{A} (\overline{BP} + \overline{BQ}) + A (\overline{BR} + \overline{BS}).$$

$$F = \overline{ABP} + \overline{ABQ} + A\overline{BR} + \overline{ABS}.$$

| AB  | 00  | 01  | ()                   | (0               |
|-----|-----|-----|----------------------|------------------|
| ACT | 0   | 2   | 81                   | \$1              |
| 0   |     | (   | ( )                  | 1                |
| 1   | 1   | 3   | 7                    | 13               |
| To  | - C | オニで | $T_3 = \overline{C}$ | T <sub>2</sub> 1 |
| 1   |     | N   | ).                   | ľ                |

Ex-2 Using n=1 MUX are can imprement los au '109, n' variable tunction and Some of "log\_N+1" variable tunctions [TIF].

Ans: 1et, 4:1 mux 50, 10924=2

Time: because the other bunctions required externel logic gates along with mux.

\* Rom (Rend only Memory).

=> Decoder + Prog. or getes } = Rom.

(Fixed And getes) (encoder)

Rom is a Combinational circuity and we can use it to implement som of minterns expression as shown in the following example:

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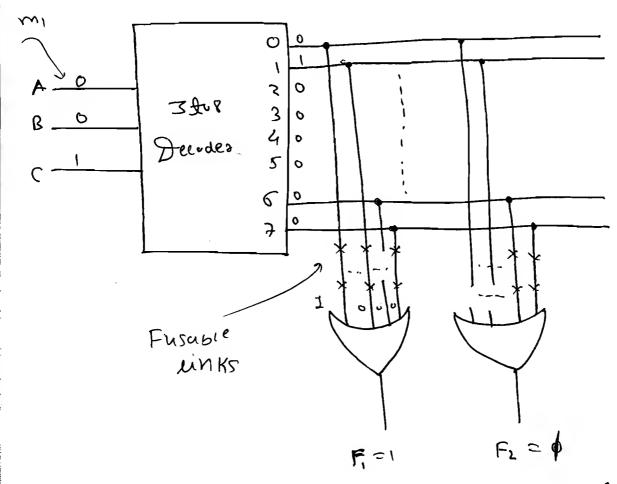
 $(\cdot)$ 

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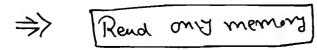
0

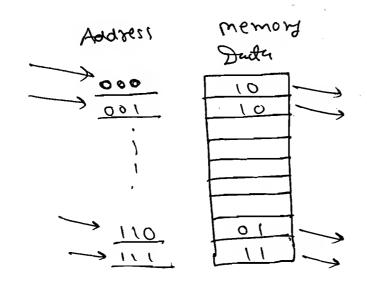
(::

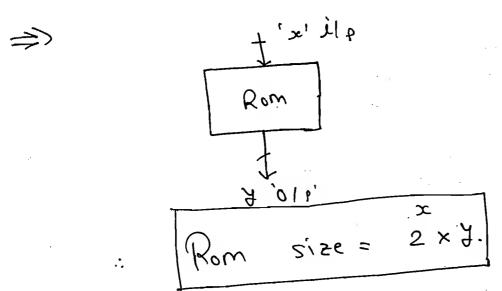
0



 $F_{1}(A_{1}B_{1}C)=$   $Em(O_{1}I_{1}A).$  Size =  $2^{3}x^{2}=16.$   $F_{2}(A_{1}B_{1}C)=$   $Em(G_{1}A).$ 







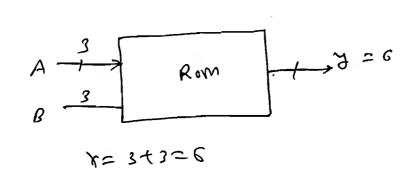
-> Rom size l'adicates fince how many bits

com be stored.

**②** 

Ex-1 Determine the size of the Rom for the tollowing tunctions.

1) Rom as 3 bit binary mutipiler.



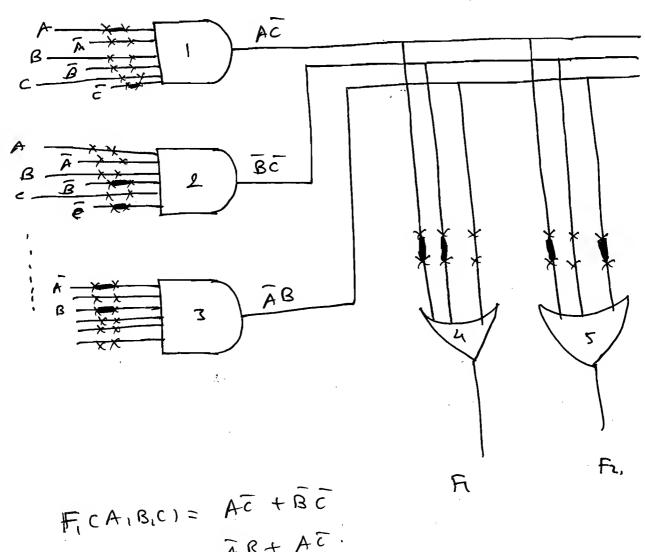
\* 71. = 49,0 Y=6 y=6 : Rom size = 2 xy = 2 x 6 = 384. cy 4-Bit squaren. Rom X=8 y = 8. Rom 1111 64x 64 15×15= 22510 27 > 225 y=8, x=4. size= 2 x 8 = 128.

2

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PLA (Prog. Logic Arrey):

Prog. AND gedes + Prog. or gedes.



F2 (ABIC) = AB+ AC.

Product term: -> P, = Ac Pz = Bc P3 = AB.

PLA size=> (3 inputs, 3 paudu(t ferms, 2 outputs).

Ex-1 In the bollowing PLA Determine the Product Learns Pi, Pz, P3, P4, P5

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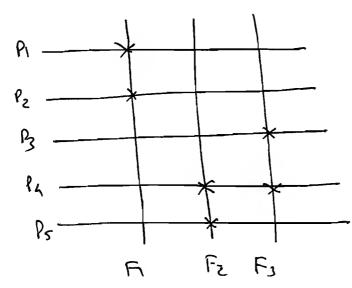
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$$F(AB(C) = \overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{AB}.$$

$$= \overline{ABC} + (\overline{BC} + B) A$$

$$= \overline{ABC} + AC + AB.$$

$$= B(\overline{AC} + A) + AC$$

$$= B(\overline{AC} + A) + AC = BBE + AC$$

$$F((A,B,C) = \overline{ABC} + ABC + \overline{AC}$$

$$F((A,B,C) = \overline{ABC} + C + \overline{ABC} + \overline{AC}$$

$$= \overline{ABC} + C + \overline{ABC} + \overline{AC}$$

Figure 1. (A,B)() = 
$$\overline{ABC} + \overline{ABC} +$$

$$F_{3} = \overline{A}B\overline{C} + B(+ \overline{A}B(-1))$$

$$= \overline{A}B\overline{C} + C(\overline{A}+B)$$

$$= AC + BC + \overline{A}B\overline{C}$$

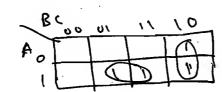
$$= AC + B(-1)$$

$$= AC + BC + \overline{A}B.$$

$$= AC + BC + \overline{A}B.$$

$$= AC + BC + \overline{A}B.$$

7



$$P_{2} = AC \qquad P_{1} = BC \qquad P_{3} = \overline{A}B.$$

$$P_{4} = \overline{A}B \qquad P_{5} = BC \qquad OR$$

$$P_{4} = \overline{A}B \qquad P_{5} = BC \qquad OR$$

$$P_{4} = \overline{A}B \qquad P_{5} = BC \qquad OR$$

\* PAL: Prog. AND geste + Fixed OR geste.

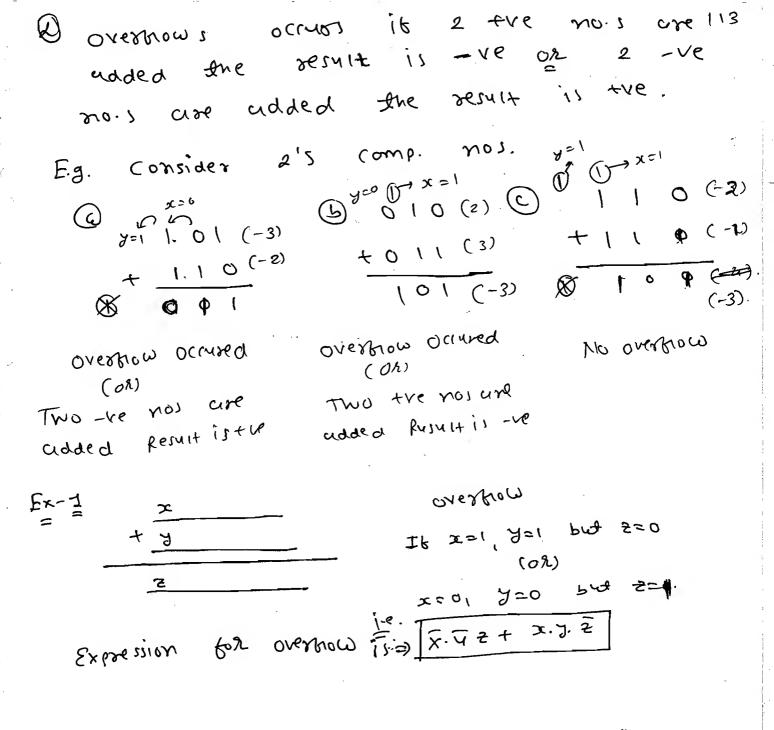
Crac: Crenenic Anny lugic

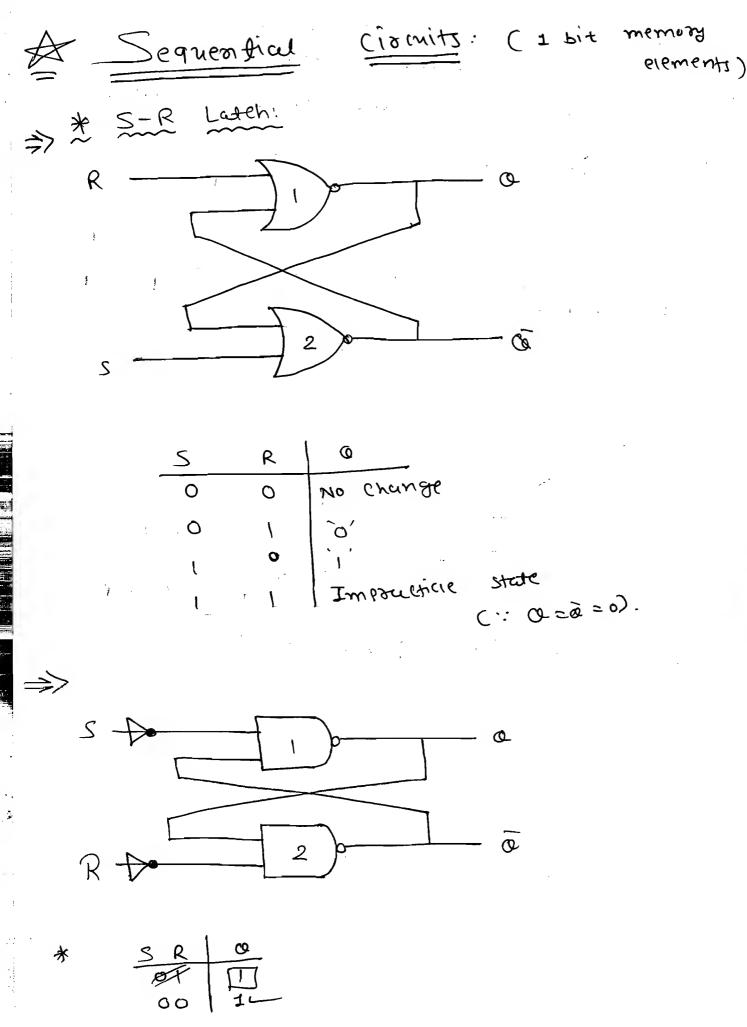
= proj. AND gestes + fixed or geste + proj. Output Logic ( E.1. Tristute OIP, Normal de etc).

How many invalid ilp combination | occur at input of BCD adders Ans: No. of Invaid BCD Empirection as Input. Total Input Combinations. - NO. of Valid Combinations. = (16x16) - (10x10) = 156. [X] [Over how:] overnow is used in signed anithmatic. -> Orestien occurr mueneres the reinit exceeds the runge ob signed nos. The overtion andition and be varitied by the following methods: sign bit and y=0 Josephow oursed. ( oh) x=0 and y=1 OVENSO W

(·)

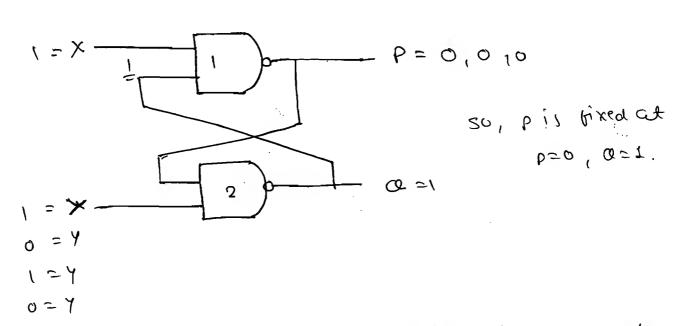
 $\Theta$ 



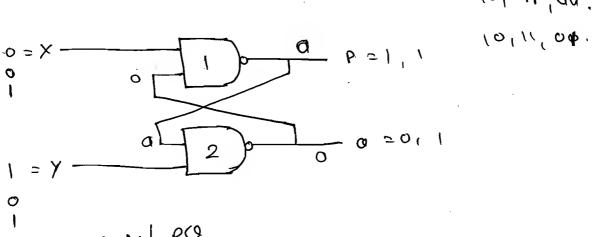


**(** 

Ex-1 In the tollowing X-4 Later initialy X=1 X=1 X=1 Determine the outputs  $P \notin Q$  If the Y input is change as O(1/011/0.11...

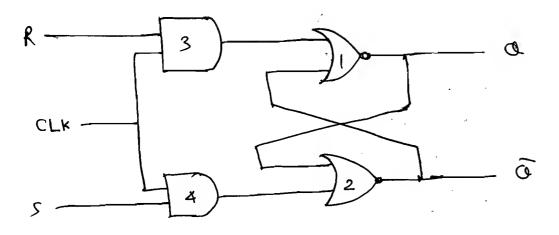


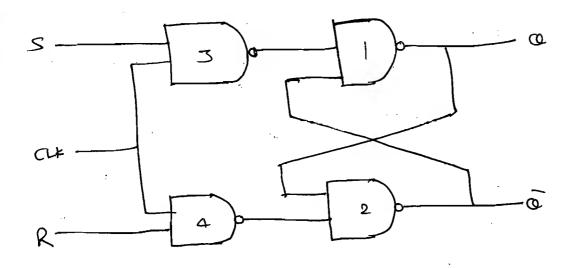
 $Ex-\frac{2}{3}$  In the following x-y Latch the sea. Of inputs are xy=01,00 and 11 - determine the values of peo.



\* clocked S-R Hip Hop:

-> Synchronized latch is caused fire-trop.





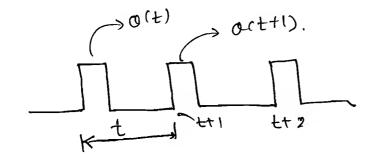
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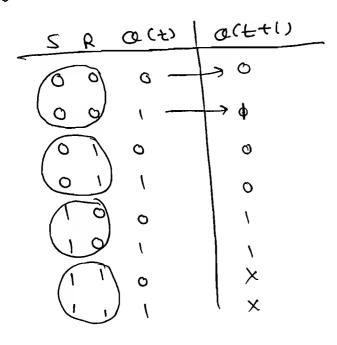
T= Clock period

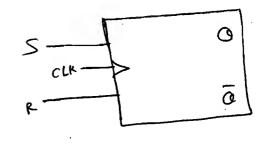
T= = Clock bea.

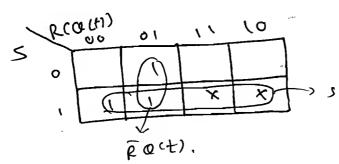


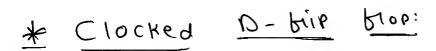
do not appy.

& Characterinic Tuble

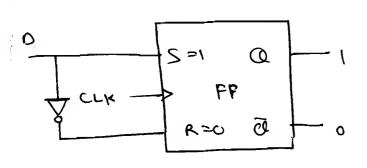


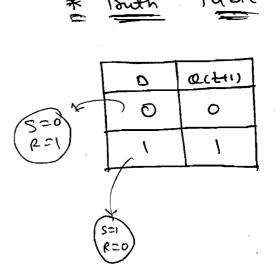






- -> used in Shift Register
- -> D -> Dester, Deray.





\* Charactertic tubie:

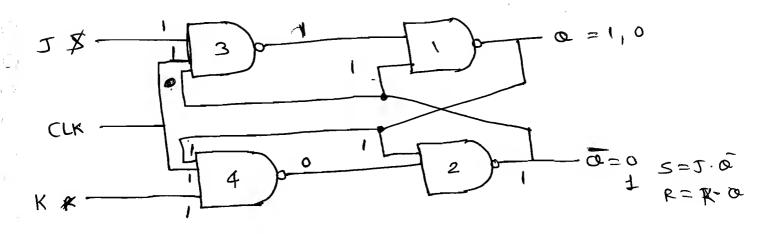
| $\mathcal{O}$ | act)       | oct+() |
|---------------|------------|--------|
| 0             | 0          | Ò      |
|               | 1          | 0      |
|               | 0          | 1      |
| W             | <i>J</i> · | 1      |

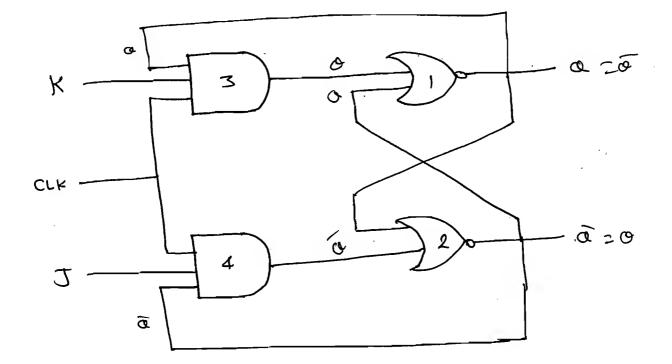
Characterstic equation.

\*

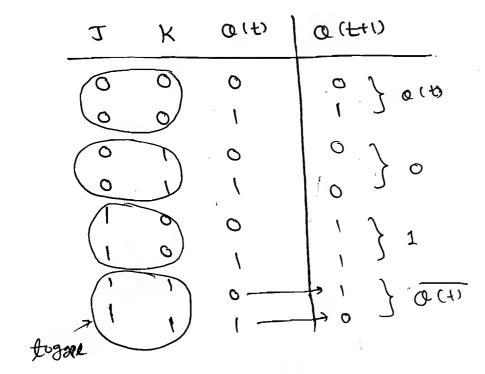
a (++1)= D.







# \* Characterstic Luble:



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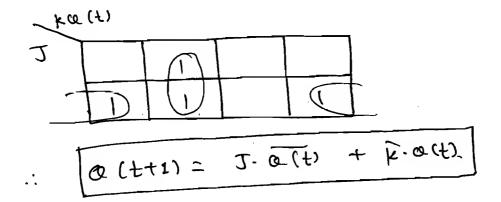
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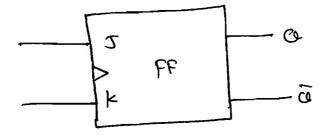
C

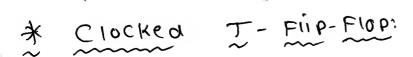
(

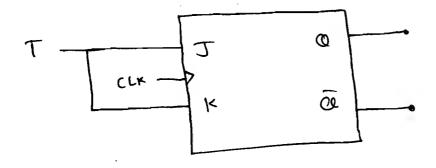
\* Characterestic temse: equation:



\*







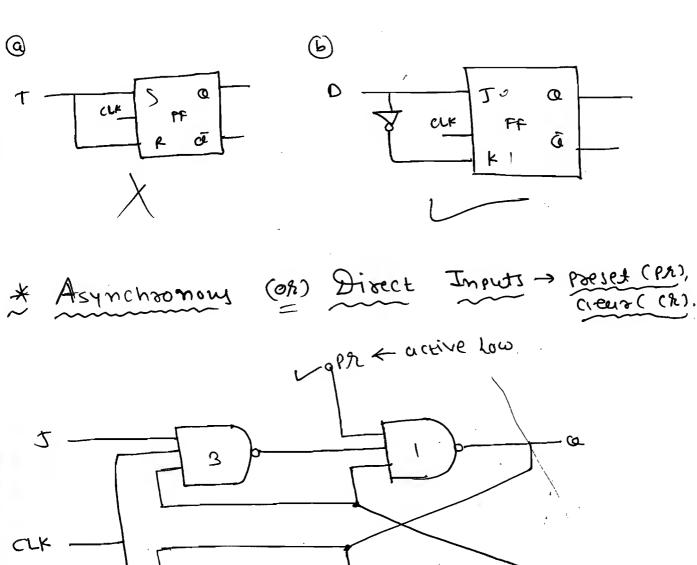
\* Touth TUble:

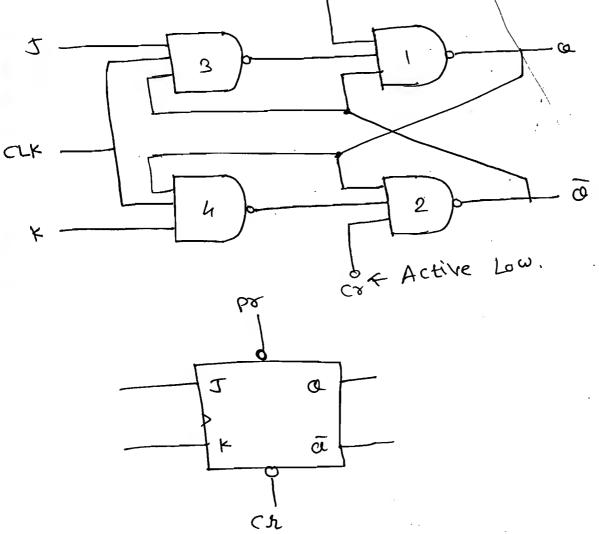
\* Characterstic Table:

| 7   | Q(4) | a (F+1)  |
|-----|------|----------|
| 6   | 0    | o > acts |
| (0) | 1    | 1 1      |
|     | 0    | 1 } a(t) |
| (,) | J    | / 0 ,    |

\* Characterstic egn:

a (++1)= T() a(+).





()

O. (% PI CLK 1 1 0 0 0 1 ٥ derends FR IIP. 1 1  $\omega$ JUL

\* Setup, Loid simes of FF.

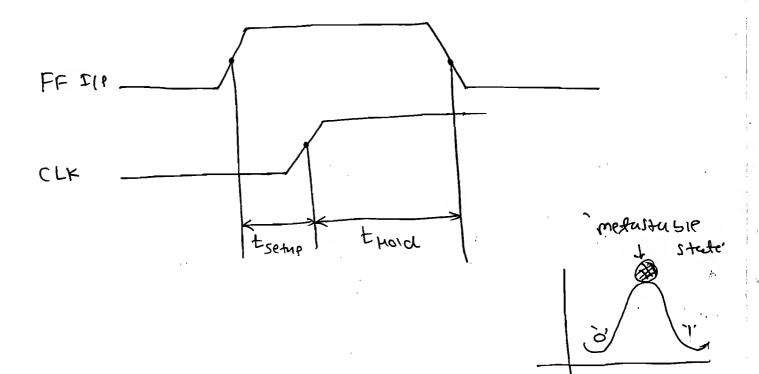
## (1) Setup time:

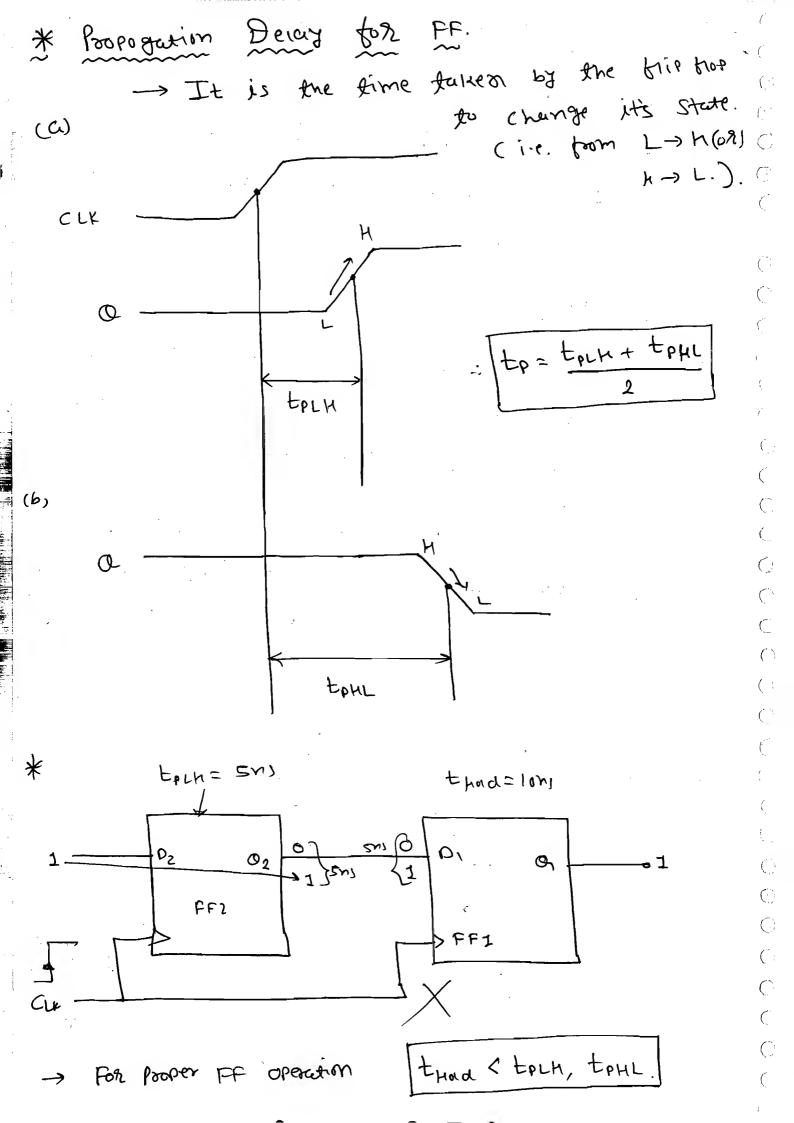
The Input Should come ahead of the Clocked input.

### (2) Hord lime:

Tt is the minimum time ton which the input Should be maintained Constant after applying the clock pulse.

-> It setup time and hold times are not Satisfies then the FF enters into metastuble state i.e. neither zero non i' output.





|   | -     |    | T          |
|---|-------|----|------------|
| * | Types | OF | Triggering |
| ~ | ~~~   | ~  | ~~~~       |

1) Level Triggered FF

2) Edge Triggered FF:

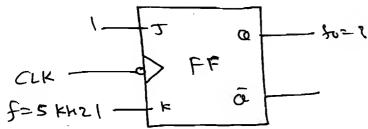
(a) Positive Edge Triggered FF

(Lending Edge Triggred FF).

(b) Negerive Edge Triggered EE

(Training Edge Triggered PF)

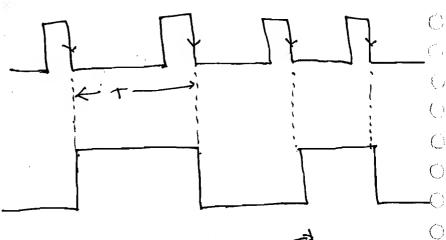
\* Determine the old freq. of following FF it the CLK beg is 5 KHZ.



#### NOTE:

$$J=k=1 \Rightarrow FF \quad jj \text{ in Togole.}$$

$$i-e. \quad \boxed{Q(t+1)=\overline{Q(t)}}.$$



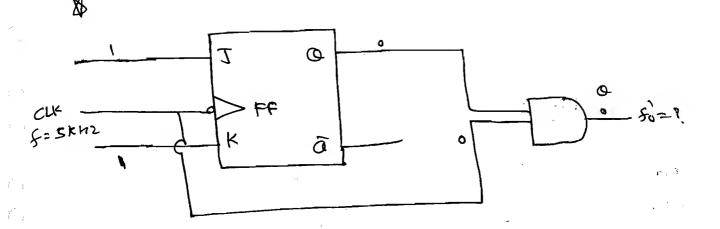
$$\frac{1}{t_0} = \frac{1}{2t} \Rightarrow \int_0^1 f_0 = \frac{f}{2}$$
 :  $f_0 = 2.5$  KH2.

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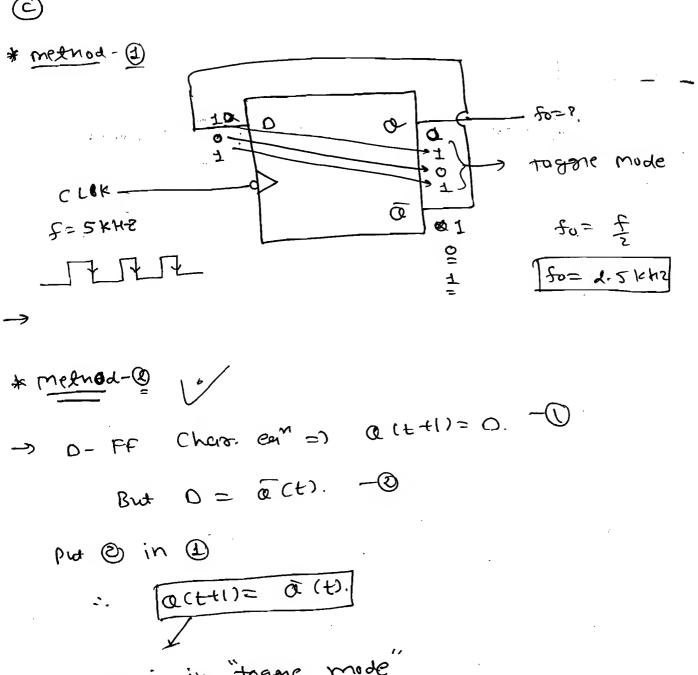


| CLK | OIP Cet Q |
|-----|-----------|
| 0   | 1         |
| 1   | 0         |
| 32  | 1         |
| 3   |           |
| 4   | 1 .       |

(b)

cux Sharing and a sharing a sharing and a sharing a sharing a sharing and a sharing a sh

: fo = 2.5kh2



Frais in "togge mod hence fo= f

:. fo= 2.5 knz

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\* Race Around Condition: (RAC). 129 -> RACE AROUND CONDETTION OCCURS IN Level trigger hip box and doesn't occur in eage triggered FFs. Dt= FF poop. delay = 2ms J O. CLK-2 K to=1001

=) "RAC" is when J=k=1 and tp>> Dt.)

-) Output Toggels manytimes instead or once.

\* How to avoid fac (in level Triggered FF).

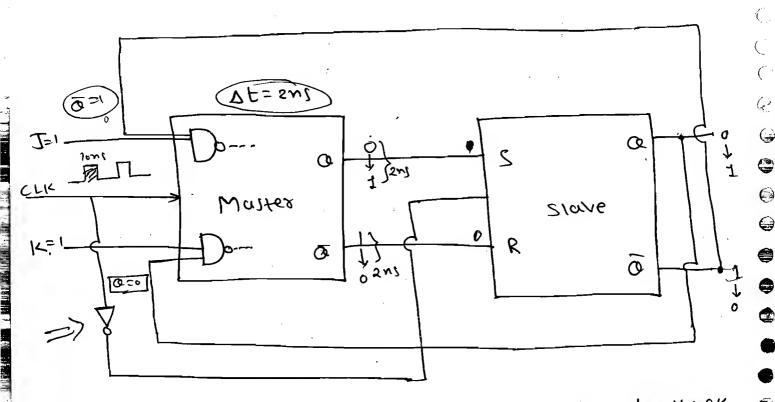
(1) Choose FF Prop delay 'At' such that.

to CDECT.

2) Master-Slave JK FF.

\* Master Slave JK FF

In master slave TK FF the teedback values a cond a do not change during the clock ruise. Eventhough the output Changes. Hence, 'RAC' doesn't occur.



→ In master slave J-k thip too the treatback

Values a cond a do not change during the

Clock pulse because they care taken from

inactive slave FF. Hence RAi doesn't occurred.

→ Master slave JK FF output is similar

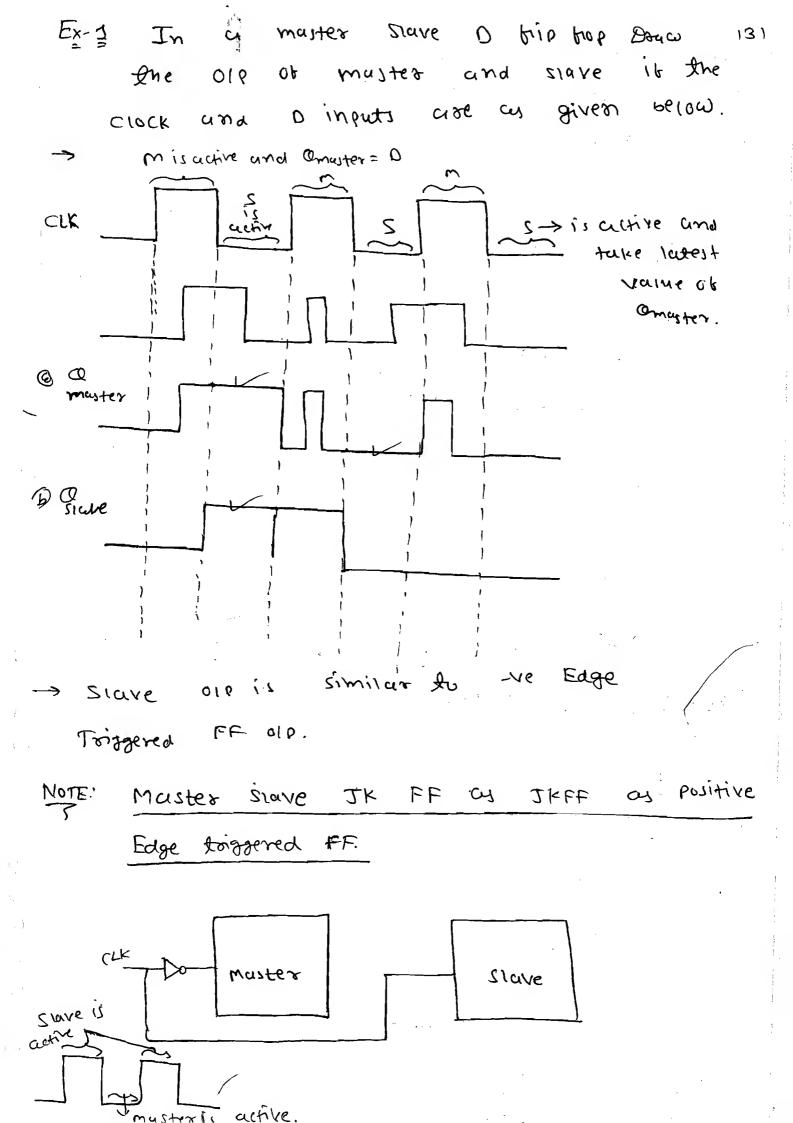
to the negative edge triggered Jk his bros

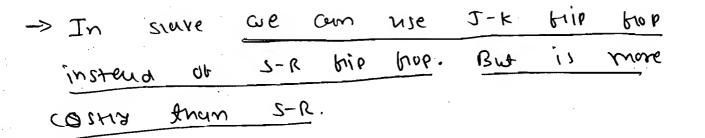
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output.





1) Shift Register - "Sequentia memory".

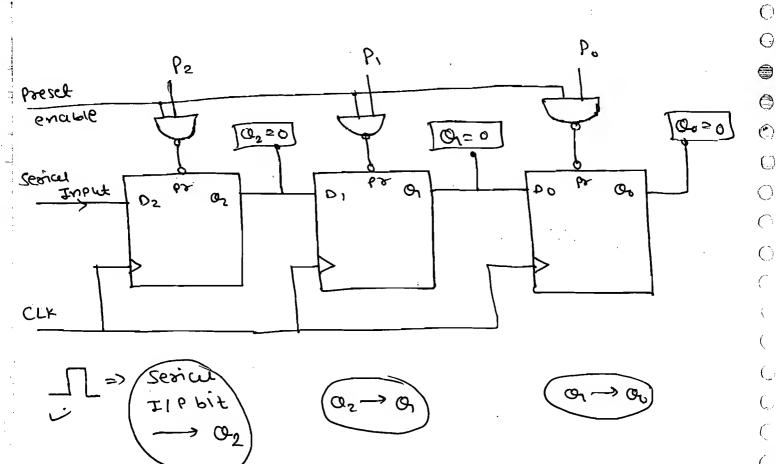
()

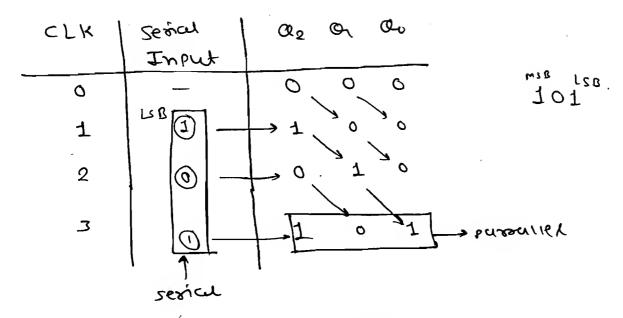
0

()

0

- @ to count the no. Of Pulles.
  - (b) Frequency Divider.



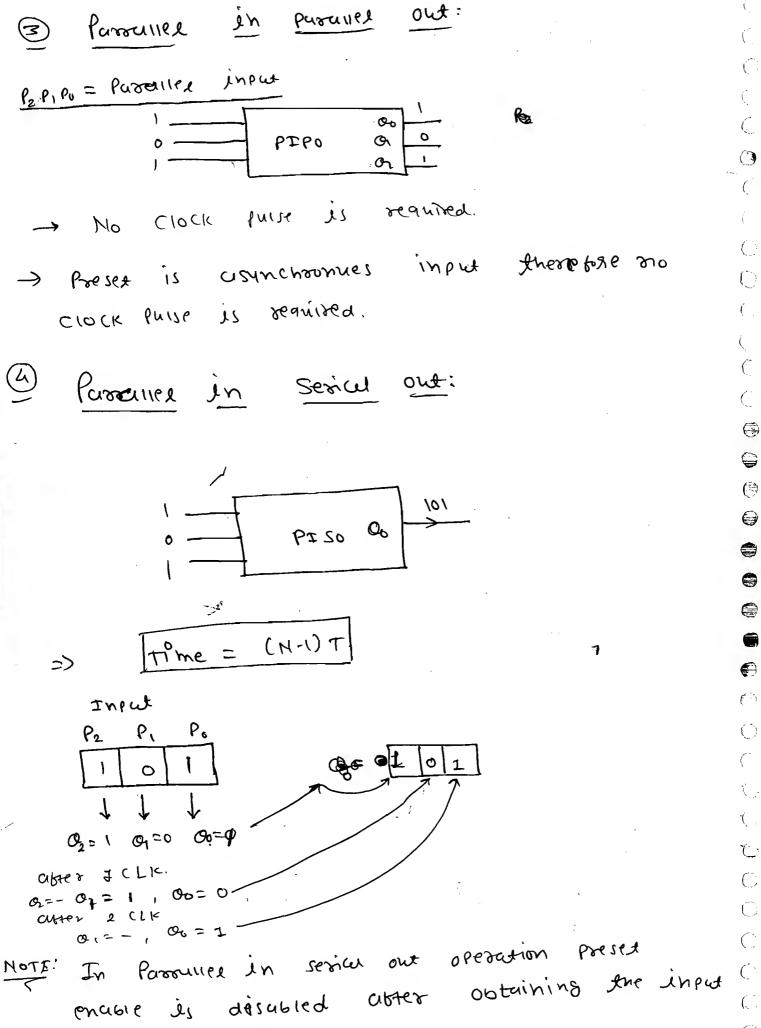


<u>Sesial</u> <u>in</u> <u>Sesial</u> o<u>ut</u>:

|                 | CLK | Sesial<br>Input | Q <sub>2</sub> Q <sub>1</sub> Q <sub>0</sub> |
|-----------------|-----|-----------------|--|
| -               | 0   | -               | 0 0 0  |
|                 | 1   | LSB             | 1 0 0  |
| Sesial<br>Input | 2   |                 |  |
| 74 box          | 3   | 1               | 1 o le sena olp.                             |
|                 | 4   | _               | 1 - 1  |
|                 | 5   | -               | 1  |
|                 |     |                 |  |

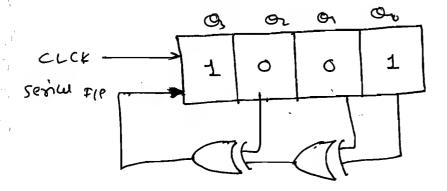
Time = (2N-1) T.

N= No- Ob FE.

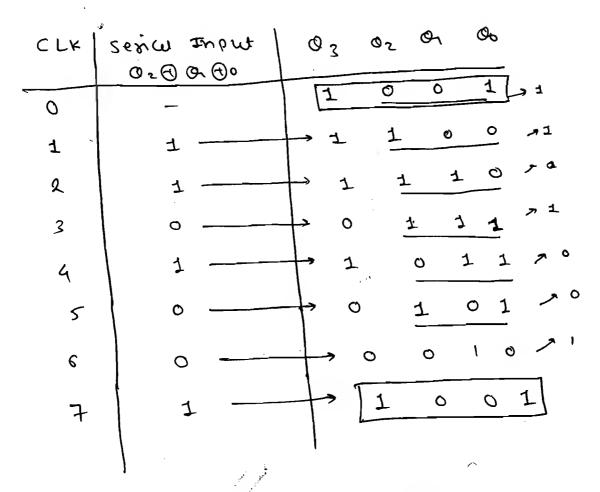


data at or, or, Oo.

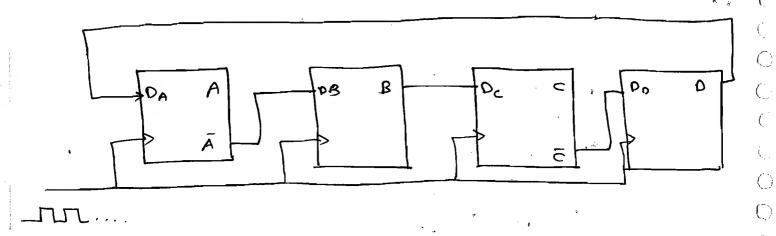
**(**. .  $\mathbb{C}$ 

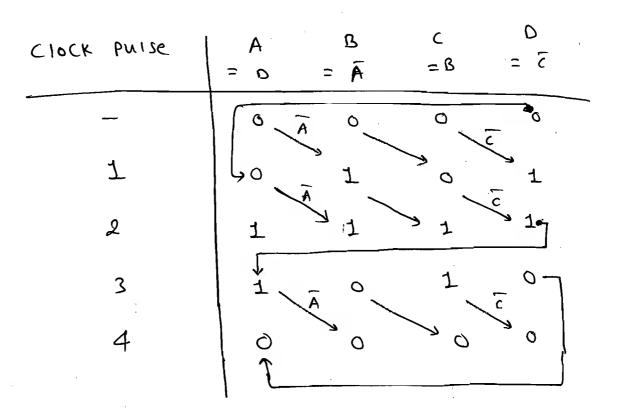


Sr. Input = 02 ( On ( O).



50, 7 CLOCK puise is required





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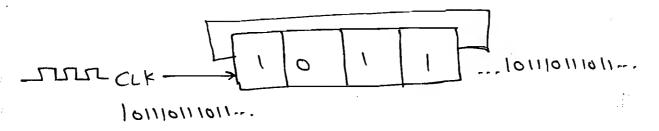
( )

O

So, After 4 Clock pulse.

\* Shift Register Application:

- 1) Serial to Paramer paramer to serial data converter.
- (2) Time delay Delay 11011... (SISO) 11011...
  - 3 Seanence Crenesator:



- (i) To generate PN (pseudo number) Semence.
  - © Ring Counter.

    © Johnson Counter.

MOTE:

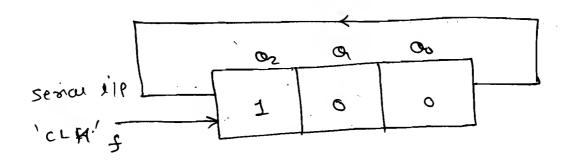
Shift Register is converted to sing

Counter by making two changes.

O do is connected to the sesich imput.

3 one ut the FF is reset.

\* 3 - Bit Ring Counter.



7.1 Counter - Can Count 3 CLK Pulses,

0

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(F)

**C** 

(j.,

(<u>)</u>,

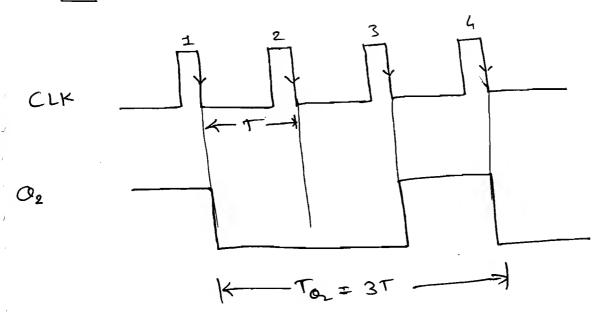
<u>(-.</u>

| clk      | serial IIP | 02 00   |
|----------|------------|---------|
| 0        |            | 1 0 0   |
| <b>9</b> | 0-         | 1 0     |
| 2        | 0          | 1 0 0 1 |
| 3        | 1          | 1 0 0   |

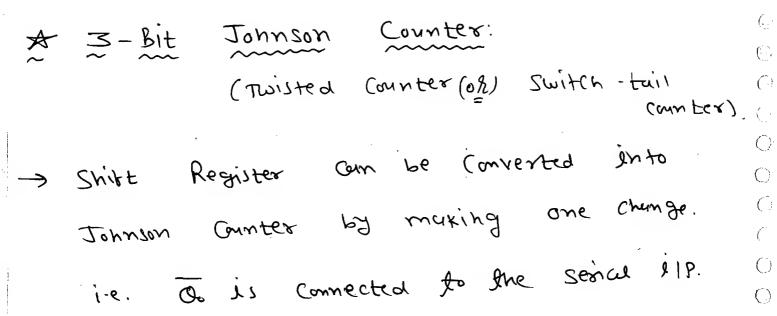
+> Connting:

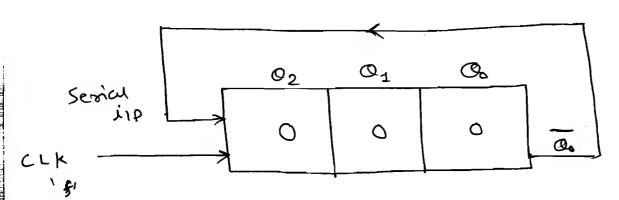
- a Ool Decode, 2 Clock Puise.
- (b) Decode, 3 CLOCK PHISE.
- © 100 Beade 1 CLOCK PHISE.

=> Frez division:



$$To_2 = 3T$$





#### 6:1 Counter.

0

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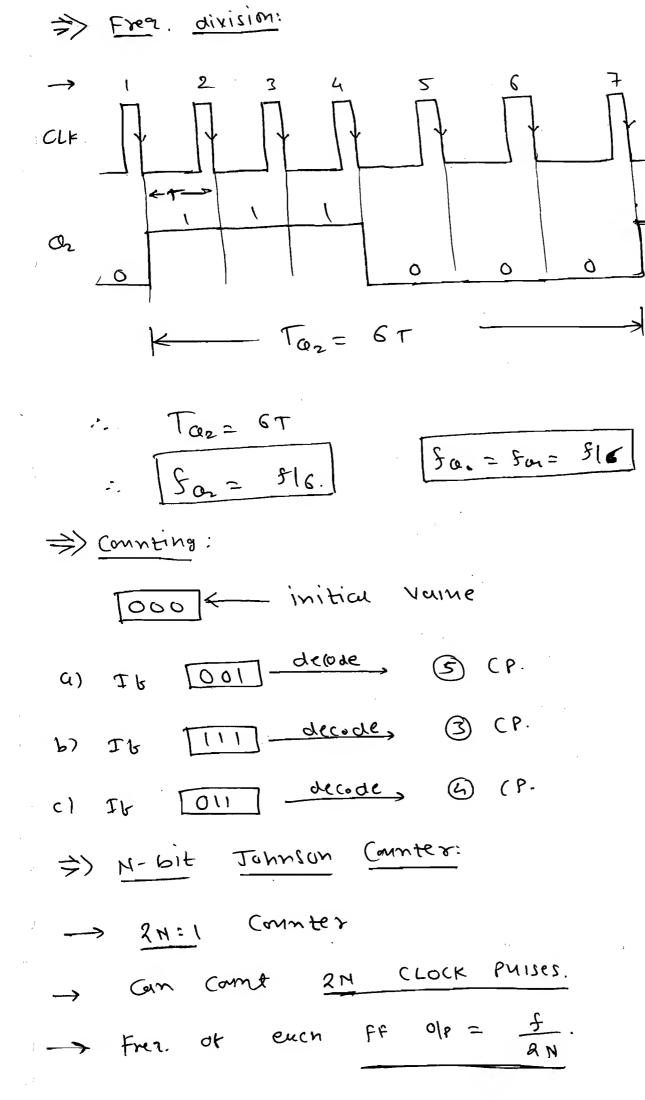
()

()

0

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| CLK | serich is To | 02 0, 00 | Decimal vaine |
|-----|--------------|----------|---------------|
| 0   | _            | 0 0 0    | 0             |
| 1   | 1            | 100      | 4             |
| 2   | 1            | 1 1 0    | 6             |
| 3   | 1            | 1 1 1    | 7             |
| 4   | 0 —          | 0 1 1    | 3             |
| 5   | ·            | 0 0 1    | 1             |
| C   | o            | 0 0 0    | 0             |



Ext Determine the Olp trez. Of a 3-bit
Johnson Counter. It the Clock trez.

Is 18 kHz. Initial Value of the
Counter is 010.

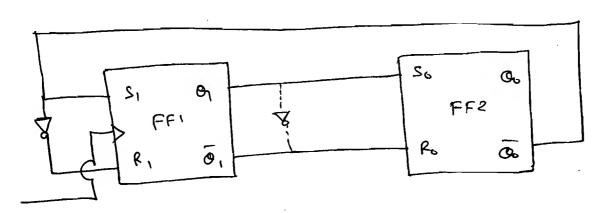
Ans:

2:1 counter.

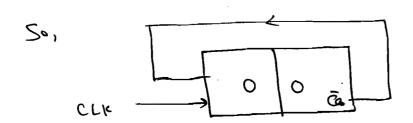
$$50 = \frac{18}{2}$$
.

Ex ? Determine the veine or the tollowing.

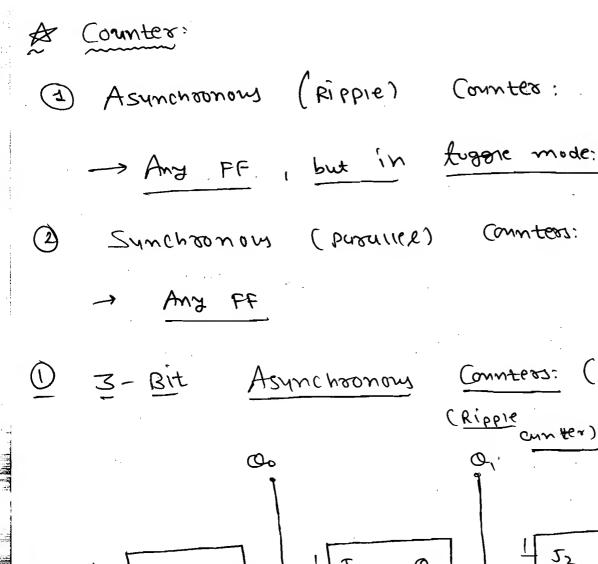
Cut after the 729 CP?

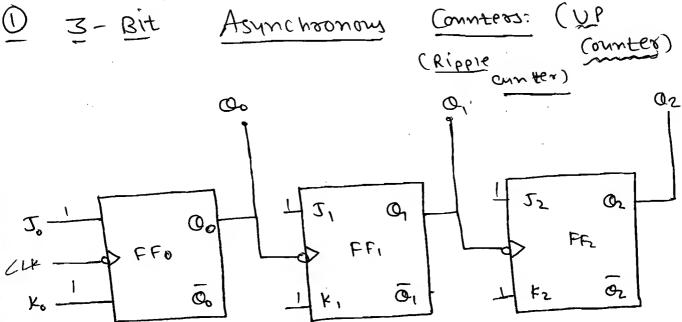


-> Given FF; are in togget mode, and use



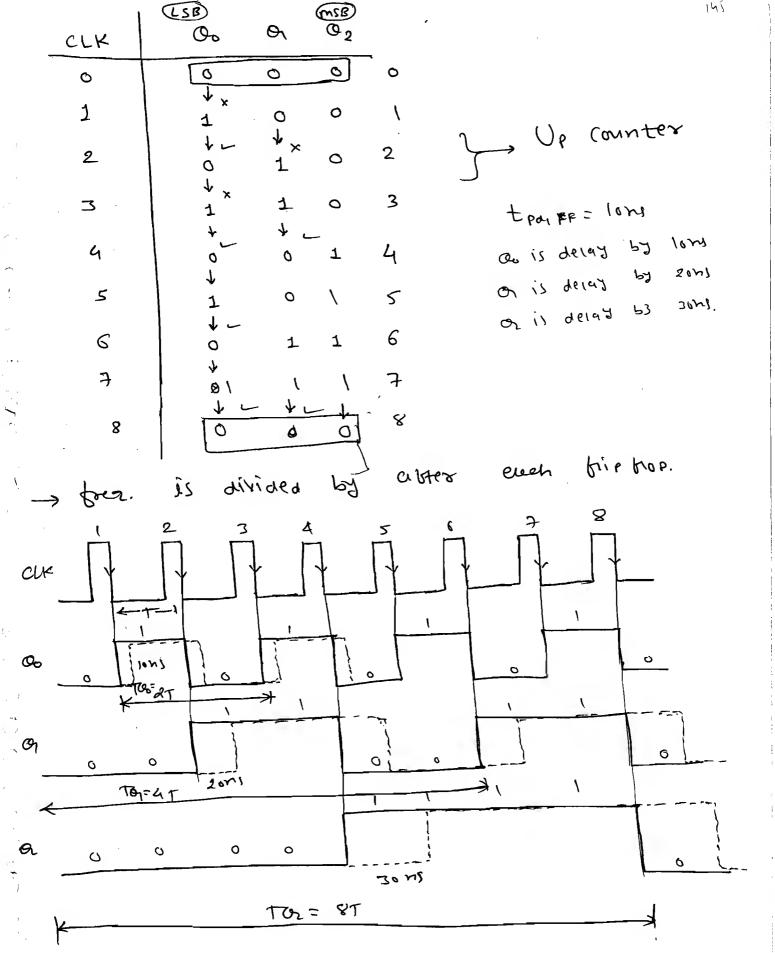
The given Counters are a 2 bit Johnson Counter honce the voine of counter after 729 CP is same on the value abter 1 CP i.e. 0=1, 0=0





$$\overline{\alpha(t+1)} = \alpha(t).$$

Of Chages from 1 tool, is togge when



\* Max. Cony. fine = 3xions = 3ons.

Clock period +> 30ms.

$$\frac{c_{3/X}}{c_{3/X}} \ge \frac{1}{t} = t :$$

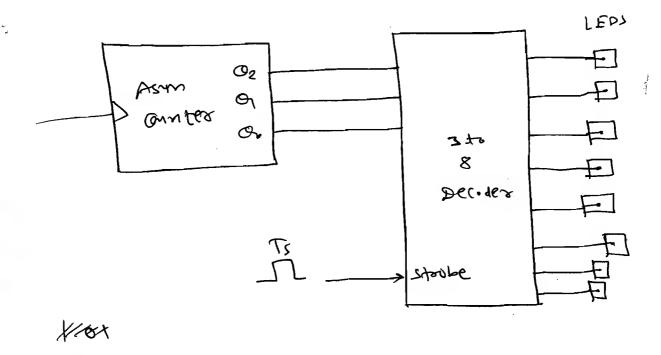
In general,

N-Bit Asynchounous Counter,

f 

N. tpd, FF.

-> Frez. ob Asunc. Counter using stooke pulse.



3 1 0 1 6 0 1 1

F < N.tpd, FF + B.

-> Asynchronomy Counter uses Stoobe

Where as Stoobe are not required in

Synchronoms.

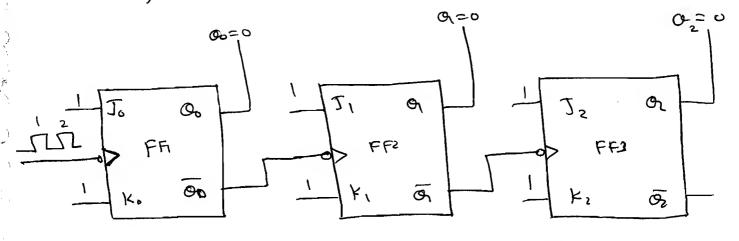
Counter).

circuits, following the

(toggles) CLOCK ton each Changes (1) Ou

fram Changes ᡐᢐ when togales (2) of 1.

fran When changes toggres 02 (3) 1. o to



| Mote: All | FG    | ax       | in t | roggie   | ~ (c     | ode.             |
|-----------|-------|----------|------|----------|----------|------------------|
| CLK       | (LSB) | <u>ه</u> | O2 1 | Deci     | mul      |                  |
| 0         | 0     | 0        | 0    | Ö        |          |                  |
| 1         | 1     | 1        | 1    | 7        |          |                  |
| 2         | o *   | \        | 1    | 6        |          |                  |
| 3         | 1     | O×       | 1    | 5        | <b>→</b> | Down<br>Connter. |
| 4         | 0 ×   | O        | ١    | 4        |          | Counter.         |
| 5         | 1     | 1        | 0    | 3        |          |                  |
| 6         | 0 *   | J        | 0    | 2        |          |                  |
| 7         | 1     | 0        | 0    | )        |          |                  |
| <         | o*    | 0        | Ò    | <b>ව</b> |          |                  |

í

 $\mathcal{I}_{l}$ J. O<sub>v</sub> () CLK FF á Q. `x'=0,1

It [x=0] => " @" is connected to the Mext FF. clock or

=> Down Counter The Red 1.0. 00,11,10,01,00,1---

[x=] => "Oo" is connected to fre Ib

Next ob CLOCK

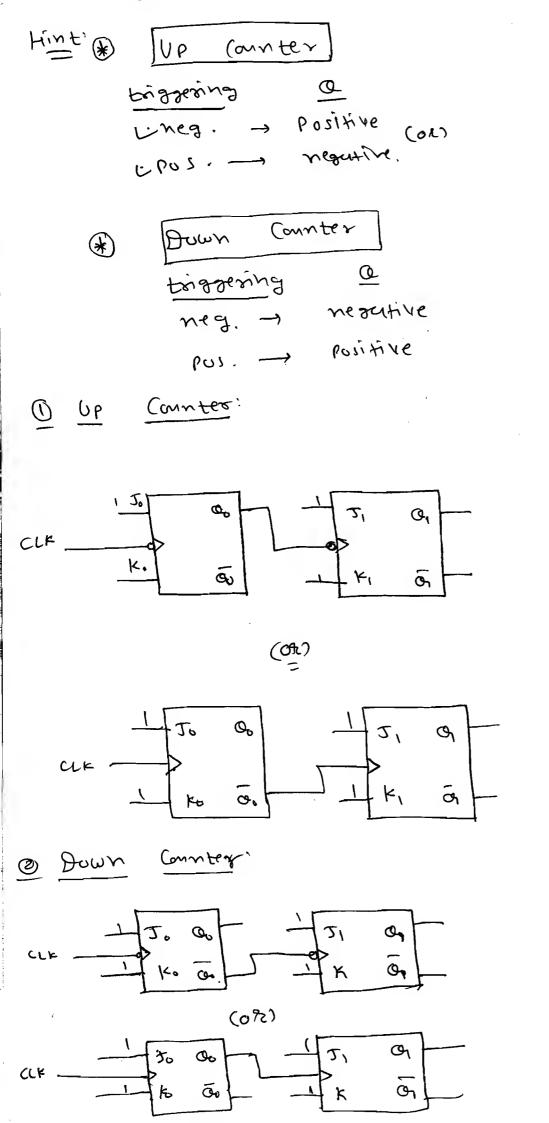
=> [Up counters

j-e. 00,01,18,11,00,00

In the above Up-Down Counter it the Imp NOTE: Linggered FF circuits then

It act of UP counter. edge x=0  $\rightarrow$ **(**)

It art of Down (anoten ' X' = 1 -**@** 



( ...

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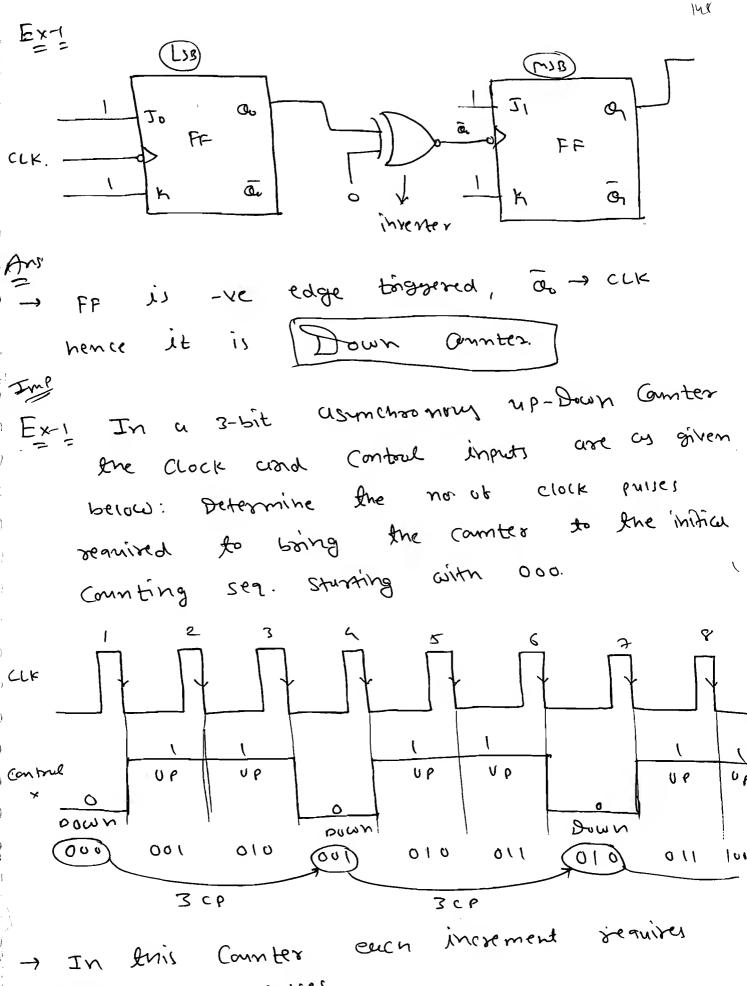
0

(. ,^.

f' . . .

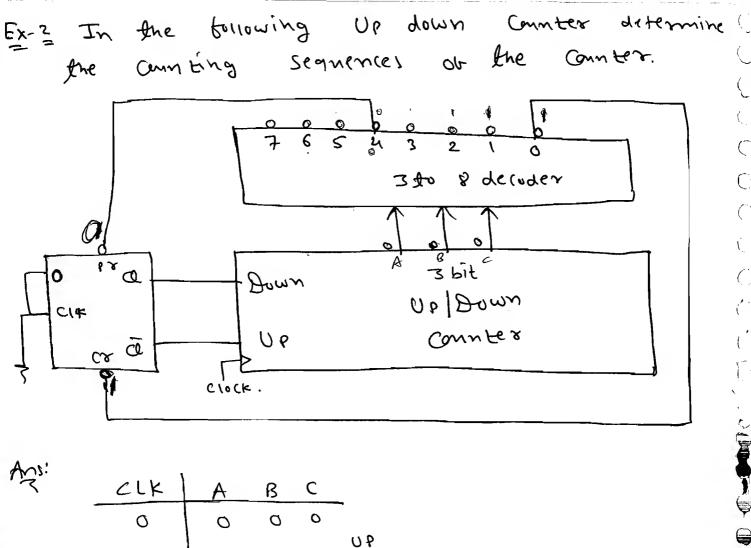
....

C



three Clock pulses. To increment 8 times No. of CLOCK

puises ure 8x3= 24.



| CLK | A B C |        |
|-----|-------|--------|
| 0   | 0 0 0 |        |
| 1   | 001   | UP     |
| 2   | 0 10  |        |
| 3   | 0 11  | O B    |
| 4   | 1 00  | UP     |
| 5   | 011   | Bown   |
| S   | 0 10  | Down   |
| 7   | 0.0   | Down   |
| 8   | 000   | Do w N |

A Modulus ob a counter.

→ It is the number Or CLK Pulses
required to bring the counter in the
initial State.

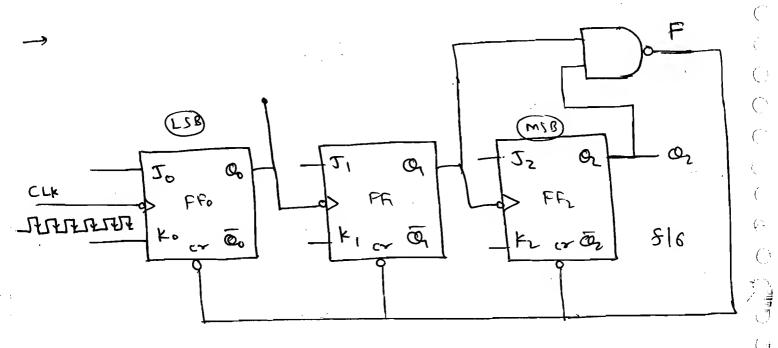
→ A Mod - N Counter Counts from 0 to N-1

Ond output freq. is 5/N.

E.g. Logic FOO gate Q3 රු 0 Or 00 On 9 0 Abter the 0 required value, 0 ı F should be 0 seso F=0. i-e for e.g.  $\mathcal{O}$ 1 o12 10 -1 ١

Constant a Mod-6 Asynchronous \*

pulse ં 6 CLK ces it remenes 800N As should be reset. jt



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C O O

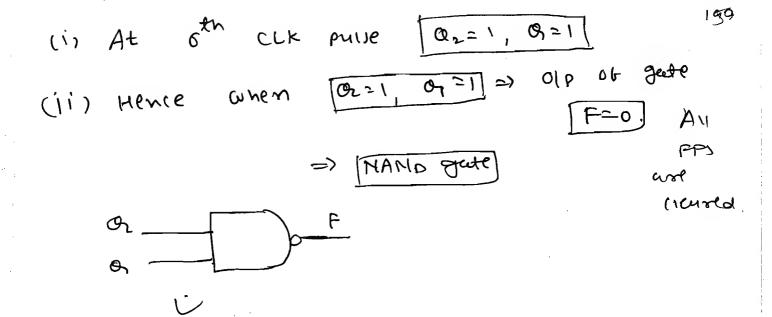
()

 $C_{I}$ 

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0

| CLK      | serial inputs | 02 On 00 | Decima |
|----------|---------------|----------|--------|
| 0        | _             | 0 0 0    | 6      |
| 1_       | \             | 001      | ١      |
| 2        | 1             | 0 10     | 2      |
| 3        | 1             | 0 11     | 3      |
| 4        | 0             | 9 00     | 4      |
| <b>©</b> | o             | 101      | 5      |
|          | O             | 1 (1)    | 6      |
|          | ,             | 0 0 0    |        |



-> In the above mod-6 asynchronous Comter determine the feedback Logic geste it its

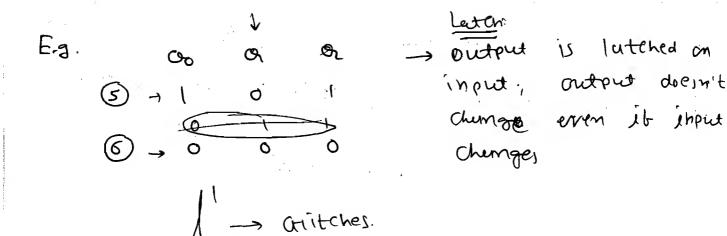
-1 i.e. Q=0 and Q=0 => 010 06 gate F=0.

\* Disudvuntuges:

→ In Asynchronous Counters whose modulys is

not concul to 2<sup>N</sup> the output produces

unwanted Spikes (and as arithmes

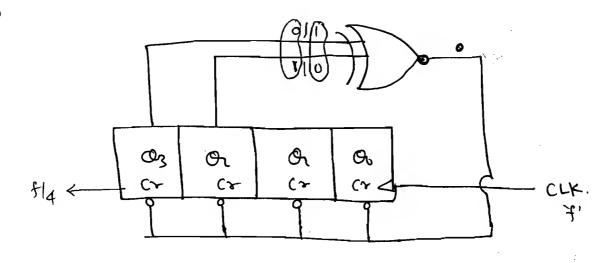


It the FF case having unequal Crowing limes then all the FFs annual be creased at the required Clack purse to to overcome this a laten is used in the beedback path such that it outnut remains zero untill all the FFS agre cleared.

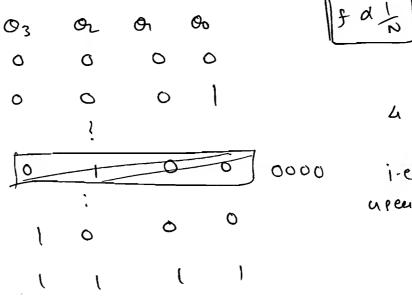
()

→ For Q3 Q20100 = 1010 → A11 the FFS are (leased.)

→ It is Mod-10 Commter (Decade Counter)



Ans:



4 will appear
list
i.e or will
upear host than

For Oz Oz Oz Oz = 0100 - All the FF3 are neured.

- It is Mod - 4 counter.

The disadvantuges of Asynchronomy Counter is the ber. of Operation is inversity proportional to the no. of FFS. To overcome this are use Synchronomy of purused Counters.

Excitation tuble: Flop O S-R FF: Q (++1) S R o(t) 0 X 0 0 1. 0 O ٥, 1. X 0 D- FUP Flop:  $\mathcal{D}$ o (++1). a (t) 0 0 0 **O**. Ţ Fiip FIOD. a (tt) T 0(4) O 0 0 0 0 0 File MOP. 4 a(ttl) J K a(t) X 0 0 X 1 6 X

0

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O C

> ( ) ( )

C C

C

|             | PF      | Inputs |   |   |
|-------------|---------|--------|---|---|
| a(t) a(t+1) | JK      | S R    | D | T |
| 0 0         | 0 X     | 0 X    | 0 | o |
| 0 1         | \ \ \ \ | .1 0   | \ | \ |
|             | × (     | 0 1    | 0 | 1 |
|             | X O     | × 0.   | 1 | 0 |

FF exitation

Ex-! Determine the exitation tube of XY FF Whose T.T. is as given below.

| ×      | 4 1 | a (ttl) | 0 (+) | a (++1) | X Y        |
|--------|-----|---------|-------|---------|------------|
| 0      | 0   | 1       | 0     | O       | X ø1       |
| 0      | 1   | Q(t)    | 0     | 1       | e ¥0       |
| ١      | 0   | € (t)   | 1     | 0       | l X        |
| ,<br>1 | ţ   | 0       | l     | l       | <b>5</b> X |
| `      | ٠.  | `       |       |         | <b>%</b> ● |

# Design a Synchronory Gunter Wing

J-k Flip Flops. which Gmes known the

States 0,1,2,4,5,6,0,...

(b) is it a selb starting Gunter?

(

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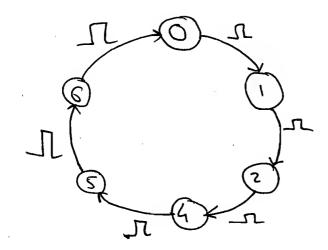
 $\in$ 

C

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 $\overline{C}$ 

Ans: (a) Strette Diagoum.



## 6 State Assignment:

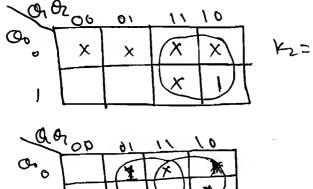
$$U \rightarrow 001$$

| <b>(C)</b> | Excitation | ruble:        |
|------------|------------|---------------|
|            | 02 0, 00   | J2K2 J1K Joko |
| (3)        | 010707     | 0 × 0 × 1 ×   |
| 0          | 0 0 0 1 1  | 0 × (× × 1    |
| 2          | 011,00     | 1 x x 1 : 0 x |
| 4          | 120100     | x0 0x (X      |
| (S)        | 1 0 1.     | XO OX AXI     |
| <u>@</u>   | 0 $1 $ $1$ | x1 x1 0x      |
| 7          | 0 00       |               |

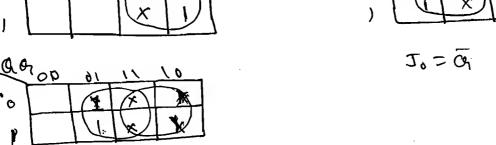
unused States. Takes them as વજ \* 3, 9 dont choes.

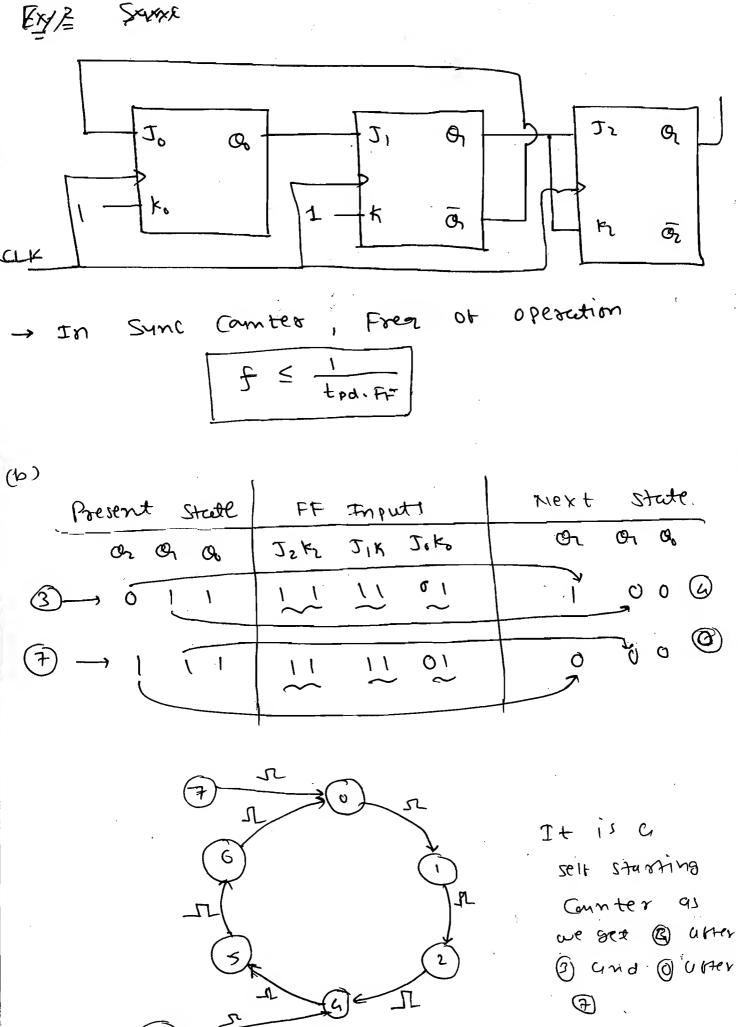
Jo= 5 k2 = 0 J2= 01

| ०० | 00 | 01 |   | 10 | i,     |
|----|----|----|---|----|--------|
| 00 | 0  | 0  | X |    | J2=01. |
| 0  | X  | ×  | x | ×  |        |
| •  |    |    |   |    |        |



J1= 9,000





()

0

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The above counter is a self starting counter because it is able to enter the used states from all unused state.

e.g. of non self starting counter

, 3

A Synchronous Counter Comes through the States 0,3,5,6,0,-- and FF inputs are Tz=a, Ti=1, To=a, Is it a Selv sturring Counter.

=> Table for analysis:

| 1           | 0 6)   | ۸۵ ۱ | <del>ر</del> ر | Input | 1    | Hext | . · · S   | itede    |                 |
|-------------|--------|------|----------------|-------|------|------|-----------|----------|-----------------|
|             | Par or | 00   | 75-19          | T1=1  | 10=6 | n or | <u>O1</u> | <u> </u> | •               |
| 0           | 0      | 1    | 0              | . \   | 1.   | . 0  | 1         | 0        | <b>②</b>        |
| <b>(2</b> ) | 0 1    | 0    | 1              | \     | 0    | )    | 0         | 0        | 4               |
| 4           | 1      | ) 0  | 0              | i     | 1    |      | 1         | 1        | ( <del>?)</del> |
| 7           |        | 1 1  | 1              | ١     | 0    | 0    | 0         | . \      |                 |

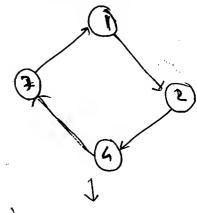
Used steete

6

3

-> It is in etricipet ounter.

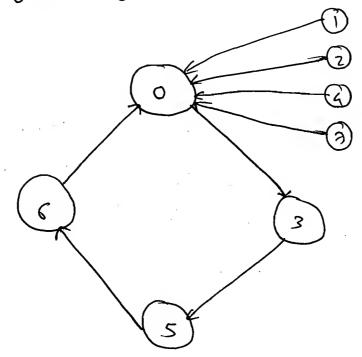
Unused Strate



North Self Sturfing Counter

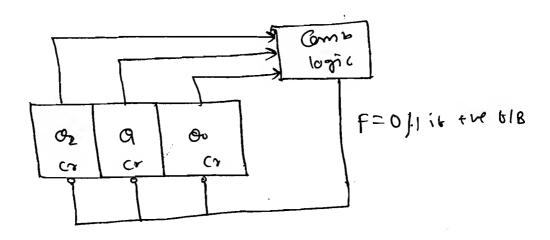
To avoid the Lock-out condition

1) Redesign the Counter according to the following state diagram.

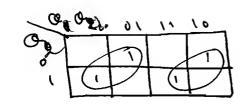


Is increased in it will increase the Comprexity of Ckt

enters into unsed state as snown below:



F(02,00,00) = Em (1,2,4,7).



F = 00 0 0000

MOLE,

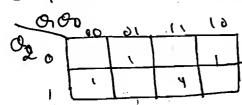
In the above synchronous counter the Combinational logic is determine as follows:

when Counter enters into the states

(1), (2), (3), (4) the F should become 1. so, that
the counter an be clear.

The sum Ob mighterm expression for Fis

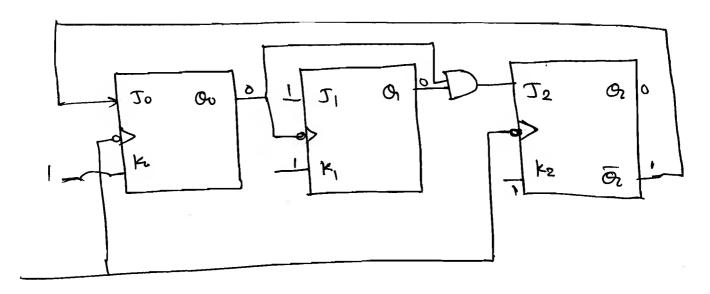
FCO2, O1, O0) = E [1, 2, 4, 9).



F= 90 00 03.

Ex-2 Determine the modulus of the bollowing

comntex



Ans: 'Q' is in Asynchronom mode. It to o:

toggne when  $O_0$  changes from I to o:  $T_0 = O_1$ ,  $T_2 = O_1 O_0$  K = 1 K = 1.

=> Table ton analysis:

| P. S. | FF I  | n puts | r+ 1.    |           |
|-------|-------|--------|----------|-----------|
| 0,00  | Jeks  | 20×0   | Or 01 00 | •         |
| 6 000 | 01    | 1 1    | 0 0 0    | (1)       |
| 0001  | 01    | 1 1    | 010      | <b>②</b>  |
| @ 010 | 101   | \ 1    | 011      | <u>3</u>  |
| 3011  | 111   | 1 1    | 100      | (4)       |
| 4 100 | 01    | 0      | 000      | 0         |
|       |       | N. S.  |          |           |
| ,     | -52 T |        | "Mod     | 4145=511. |

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C (

> (. . .

> > *-* :

0

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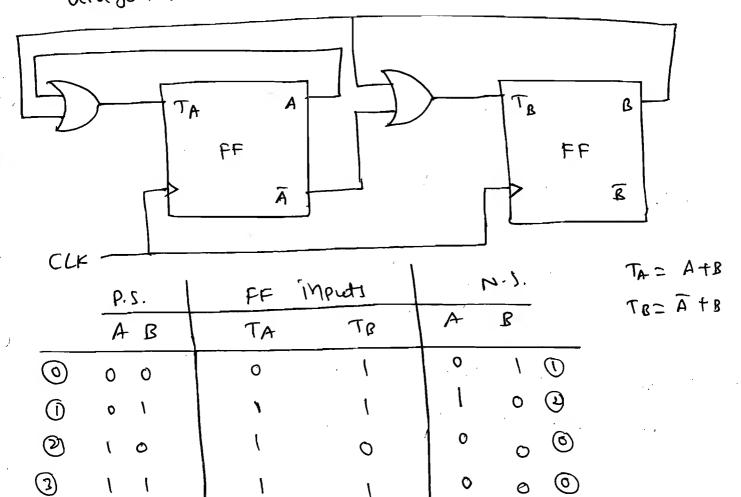
() (' Max. (onv. fime = 10+10= 2001.

C: FFo, FFz use in synch. mode, FFI is in Async mode].

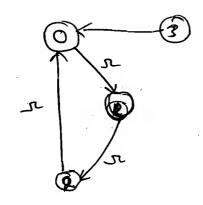
Clock Period [T > 2011.]

$$\int_{\text{max}} \frac{1}{20 \times 10^{-9}} \text{ hz}$$

Ex 3 Determine the th ob the following Sea. Circuits by obtaining its state diagram.



## State diagoum'



→ it is a MOD-3, self sturting synchronous
Counter.

## \* State Diagram:

HINT'

(i) No of States = 2; N= Mo of FFS

 $\Theta$ 

0

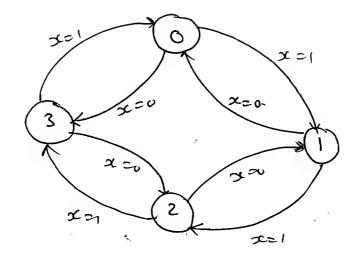
(ii) No or paruches from ouch state = 2x;

1) 2-Bit UPIDOWN SYNC CONNTER:

-> RFF1 => No. Of States = 22= 4.

( Q, Q, = 00, 01, (0,11)

even state = 21:=12.

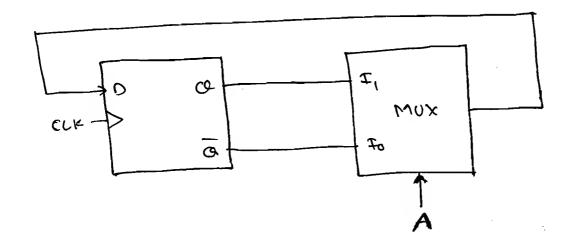


Stute Diugoum]

$$\rightarrow$$
 1 FF  $\Rightarrow$  2 States ( $\alpha = 0$ ,  $\alpha = 1$ ).

|        | Ø (F) | 2 | k   | alth |
|--------|-------|---|-----|------|
|        | 0     | 0 | 0   | 0    |
|        | 0     | 0 | ţ   | 0    |
| 00,10  | 0     | ι | 0   |      |
| (0=0)  | 0     | Ž | 1   | 1    |
| 61,11. | 1     | a | 0   | \    |
|        | 1     | 0 | 1   | 0    |
|        | 1     | ١ | 0   | 1 (  |
|        | 1     | , | 1 1 | 0    |

3 Greate - 2013



-> I FF => 2 state.

POR 0-FF -) Q(++1)=D -0

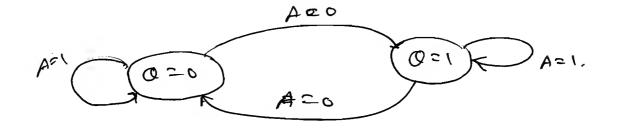
FOR MUX = D= A. a + AQ. -2

born - 0 & 0

.. O (++1)= A.Q(t) + A-Q(t).

onen A=0, a(t+1)= a(t)

A=1, action action



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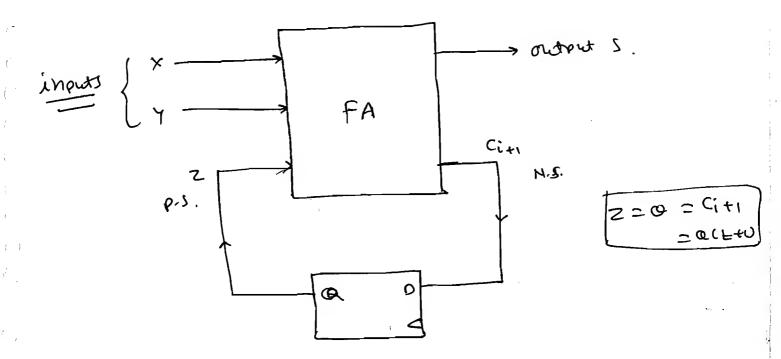
(),

( (

C

C.

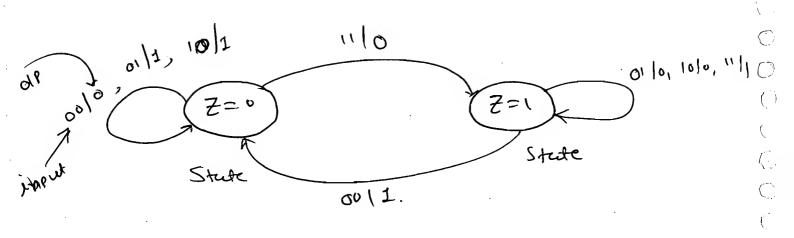
( ) ( )



-> 2/1XXXXXX 1 FF -> 2 States (2=0, ==1).

 $\rightarrow$  2 input  $\rightarrow$   $2^2 = 4$  bouncher form each state.

| P. S. | input ] | N·3.      | output |
|-------|---------|-----------|--------|
| (2)   | × ~     | C; +1     | Sum    |
| 0     | 0 0     | 07        | 0      |
| 0     | 01      |           |        |
| 0     | 10      | [0]       | \ \    |
| ·. o  | 1 1     | 13        | 0      |
| 1     | 0 0     | 1.03      | ,      |
| 1     | 0 1     | 101.      | 0      |
| 1     | 10      | -   · · ( | ( ) 0  |
| 1     | 1 1     |           | ]      |



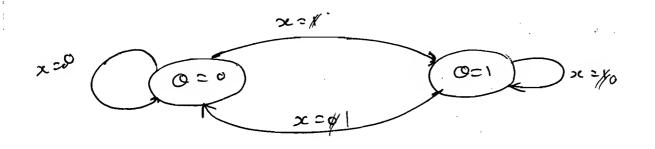
0

0

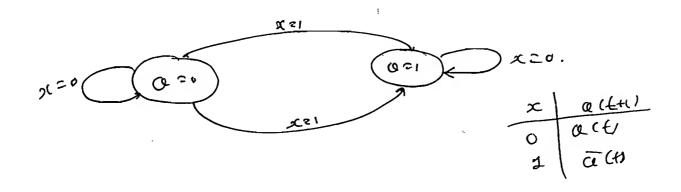
 $\bigcirc$ 

 $C^{-}$ 

Ex-1 Identity the following FFs.



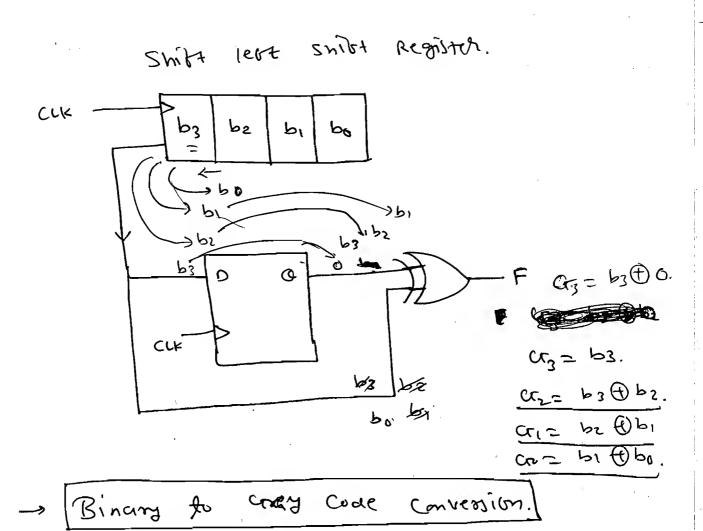
| × | act+1) |
|---|--------|
| O | 0      |
| 1 | 1      |
|   |        |

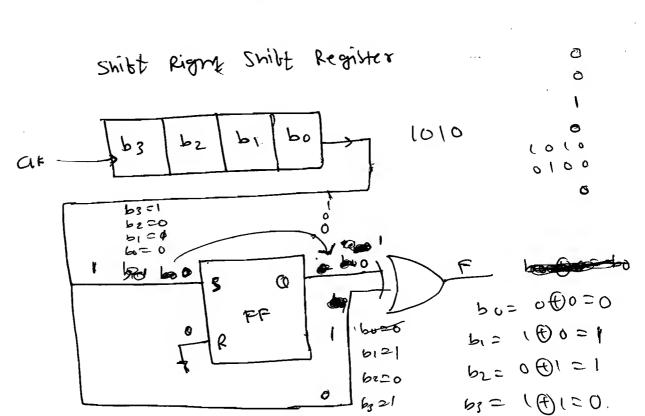


Ex-1 Determine the 6" of the tolowing 165 circuits.

(1)

2)





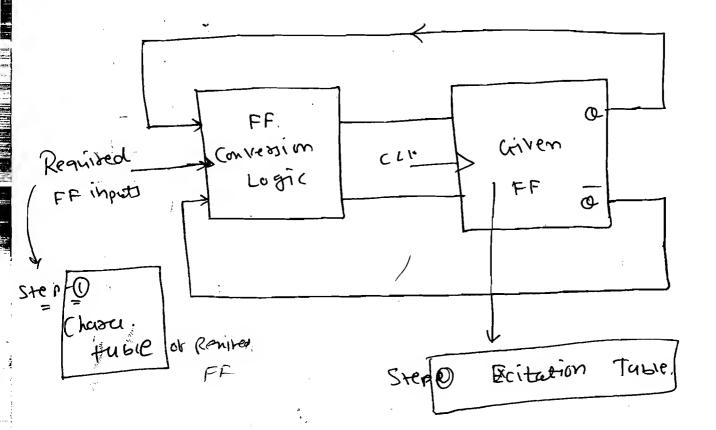
Input = [1010]

- It is 2's comp. of binary no.

> 50, [it is 2's comprement circuit

\* Conversion of Fliptiops:

=> Universal Principie:



()

0

 $\binom{n}{k}$ 

 $\in$ 

162.

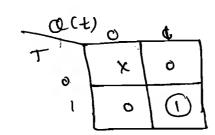
Ex-1 Convert

Ans:

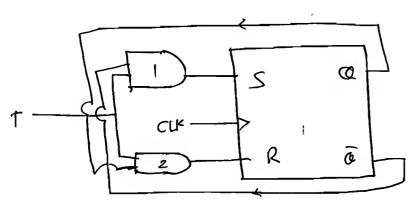
Step - O - Characterestics tuble 06 T-FIR Hop.

Step-@ -> Excitation tubic of 12 hip hup.

|   |     |      |               |   | 7             |
|---|-----|------|---------------|---|---------------|
|   | T   | a(f) | a (++1)       | 5 | $\frac{R}{R}$ |
| 1 | (0) | 0 —  | <b>&gt;</b> 0 | 0 | ×             |
|   |     | 1 _  | 1             | × | 0             |
|   | (1) | 0 _  | 1             |   | 0             |
|   |     | 1    | \_``o         | 0 | 1             |
|   | l   |      |               |   |               |

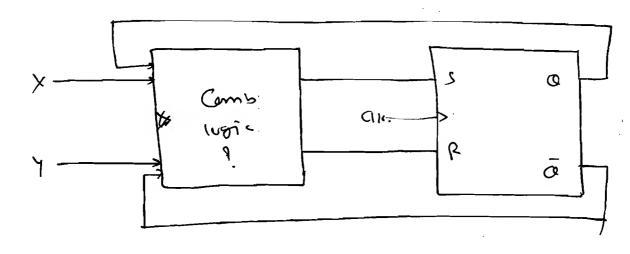


R= Ta(+).



[T- Fir FLOD]

Ex-2 In the torowing diagram determine the Combinationa logic to be used.



000000000

0

()

Û

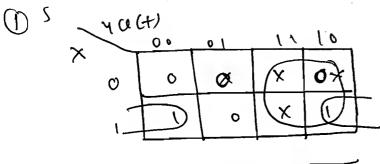
0

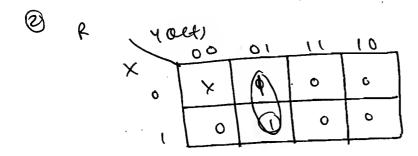
()

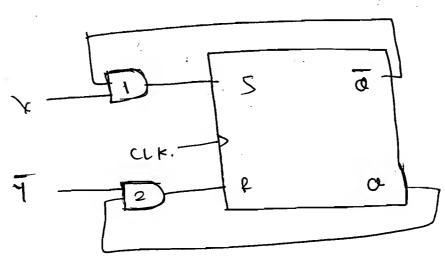
(cryens)

| X4 \ | @ (tt) | SR |
|------|--------|----|
| 00   | 0      | \  |
| 0 1  | (d)    |    |
| l 0  | ( C+1) |    |
| l /  | 1      |    |

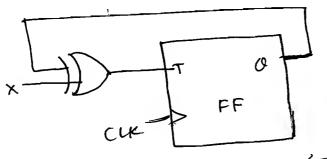
|            |   |      |        |   | 8   | P          |   |
|------------|---|------|--------|---|-----|------------|---|
|            |   | Q(t) | a (+1) |   | S   | P          | _ |
| ~ <u>~</u> |   | 0    | 0      |   | O   | ×          |   |
| O          | 0 | J    | 0      | 1 | χO  | 01         |   |
| 0          | 0 | 1    |        |   | O   | ×          |   |
| 0          | 1 | 0    | a      |   | · · | <b>7</b> * |   |
|            | 1 | ١    | l      | 1 | X   | 0          |   |
| 0          | , |      | 1      |   | \   | 0          |   |
| 1          | 0 | O    | •      |   | Ø   | 1          |   |
| 1          | 0 | 1    | 0      | 1 | 1   | 0          |   |
| 1          | 1 | O    | 1      | 1 | ,   | O          |   |
| )          | 1 | (    | ł      |   | ×   | 0          |   |







Ex-3 Identity the following hip trop.



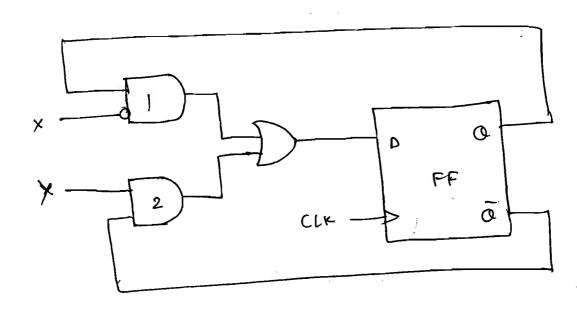
$$T = x \Theta \alpha(t) - 0.$$

FOR T PF T=) a (H1)= T() Q4)

act+1) = 20 act 1 6 act)

(De Know => 3) is similar to D-FR Charger

6)



$$0 = 0 \times + 0 \cdot$$

$$0 = 0 \times + 0 \times + 0 \cdot$$

$$0 = 0 \times + 0$$

So, jt is J-K hip hop.

171 <u>5</u>. - Tu-Supt auctor BUISH AI B Person ours. = ABB[Li+ABB] ABB <u>o</u>. ABB+ Bit ABB (AOB) bi B= 51 (AOB) - A ① B ① bi

B = A (A) B (A) bi

B= 6 (AOB) + AB

4 7 8

۵. D 1) A+ AB 8. A8 8. A82 7. A.8 1) A + Bl 1) ij A+ A3 = A5 **y**. 61. A⊕B 5 Ø bi (AOR) + AB = bi. (bi. (AB) bi + bi (A()8) A 0 8 - bi bi + AAB Ø ھ DO A &

<del>\*</del>

| N

Subtractor

ZAZD

gate

RIVO

B= bi (ADP) + AB,

D= A ABA b;

Ù Citi = C: (ABB) + AB S= ABBBG W AB AAB A Pos હ્મ, CICABB) C; (A + AB 40 CHI CI (ABB) + AB S= ABBBC;

17.00 \* Tull

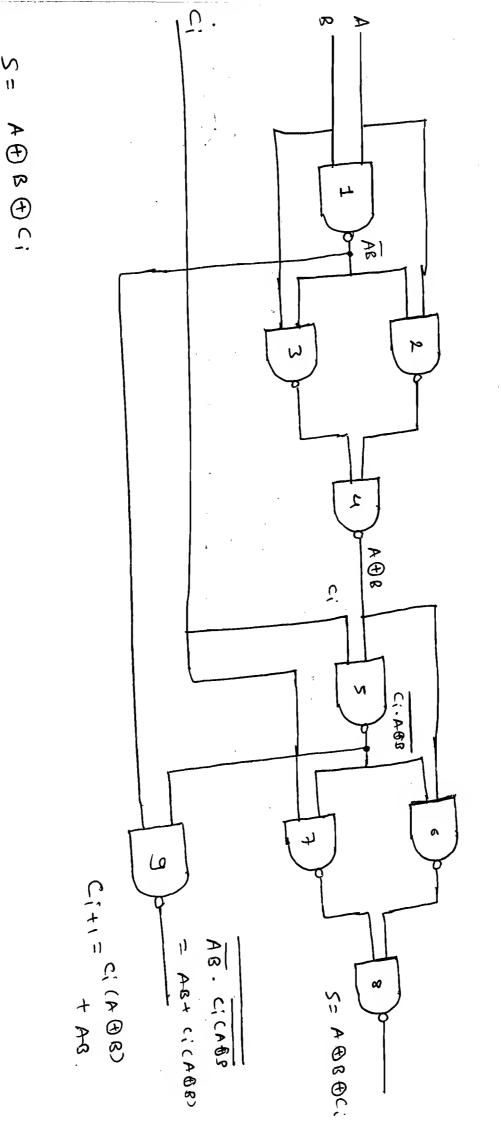
Adder

BHISM

No.P

Rived Davis.

\* Full adder Buisna NAND gut RIKO



*(*)

Ci. (AAB) + AB

**V** 

